ECON G6905 Topics in Trade Jonathan Dingel Spring 2025, Week 1



# Outline of today

- ► Introduction + logistics
- ► Overview of the course
- ▶ Brief introduction to trade theory
- ▶ The CES Armington model of international trade

# Logistics

This class

- ▶ Wednesdays, 8:10-10:00, IAB 1101
- Jonathan Dingel
  - ▶ Email: jid2106@columbia.edu
  - ▶ Office: IAB 1126B
  - ▶ Office hours: By appointment, please email
- Course materials: github.com/jdingel/econ6905 and courseworks2.columbia.edu

Broader context:

- This class is the economic-geography bridge between Weinstein's trade class and Davis's urban class
- ▶ I will emphasize computational aspects
- You should attend the Trade and Spatial Colloquium (Wednesdays, 12–1, IAB 1101)

### Assessment

My goal is to introduce some concepts and tools in international trade and economic geography so you can tackle relevant research questions

- Grades based on assignments (70%) and a final exam (30%)
- ▶ Three types of assignments
  - Economics: Derive a theoretical result or survey an empirical literature.
  - Programming: Write a function that solves for equilibrium or estimates a parameter.
  - ▶ Referee report: Assess a recent working paper.
- ▶ Final exam at end of semester

Grab assignments from GitHub. Submit your work via Courseworks.

# Coding

Submit transparent, self-contained code:

- Your code must reproduce your work in the "just press play" sense of the AEA Data Editor
- ▶ You may use Julia or Matlab. Use Julia.

See my recommended resources webpage for suggestions.

- ▶ Grant McDermott Data science for economists
- ▶ Ivan Rudik AEM 7130 Dynamic Optimization
- Paul Schrimpf and Jesse Perla Computational Economics with Data Science Applications
- Jesus Fernandez-Villaverde Computational Methods for Economists

▶ Perla, Sargent, Stachurski - Quantitative Economics

How many have used: Matlab? Julia? Git? Build automation?

# Objectives

- My goal is to prepare students to tackle research questions in trade, spatial, and urban economics
- ▶ Writing papers is about matching skills with opportunities
- In my experience, spotting opportunities is a hard-to-teach combination of insight and luck
- This class will aim to equip you with skills so your technical quiver is full when you spot a target

# Topics

- 1. The CES Armington model
- 2. Gravity regressions
- 3. Increasing returns and home-market effects
- 4. Non-homothetic preferences
- 5. Agglomeration economies
- 6. Quantitative spatial models
- 7. Quantitative urban models
- 8. Exact hat algebra and calibration
- 9. The canonical urban model
- 10. Spatial sorting of skills and sectors
- 11. Discrete choice estimation and simulations
- 12. Multi-region firms
- 13. Spatial environmental economics

See my comments on "Linkages between international trade and urban economics"

### Why trade and spatial are interesting

- International trade has long intellectual history (Smith, Ricardo) and is hot policy topic today (Brexit, Trump)
- ▶ Healthy balance of theory and empirics (c.f. theory-dominated from 1817 to 1990s) in which each informs the other
- Trade has tools and insights relevant for topics ranging from intracity commuting to national TFP growth
- ▶ I used to say trade economists sometimes have a data advantage because governments track cross-border transactions
- Spatial economics is a small but rapidly growing field (e.g., The rapid rise of spatial economics among JMCs, UEA history)

#### Why are you interested in trade/spatial/urban?

This week, we start with international trade

# Why trade and spatial are interesting

- International trade has long intellectual history (Smith, Ricardo) and is hot policy topic today (Brexit, Trump)
- ▶ Healthy balance of theory and empirics (c.f. theory-dominated from 1817 to 1990s) in which each informs the other
- Trade has tools and insights relevant for topics ranging from intracity commuting to national TFP growth
- ▶ I used to say trade economists sometimes have a data advantage because governments track cross-border transactions
- Spatial economics is a small but rapidly growing field (e.g., The rapid rise of spatial economics among JMCs, UEA history)

Why are you interested in trade/spatial/urban?

This week, we start with international trade

# Trade's interplay between theory and empirics

Descriptive facts motivate theoretical work

- Observed intra-industry trade motivated "new trade theory" (e.g., Krugman 1980)
- Observed firm-level heterogeneity motivated "new new trade theory" (e.g., Melitz 2003)

Empirical evidence comes from wide range of methods

- Descriptive statistics
- ▶ Estimated/calibrated quantitative models
- ▶ Applications employing sufficient statistics
- Quasi-natural experiments (rare, but see Japanese autarky, Suez Canal, the telegraph, etc)

Testing is tricky: See Harrigan (2001) and Adao et al (2023)

- ▶ Is it a "test"? Is there a clearly specified alternative hypothesis?
- ▶ How does the test isolate the distinctive GE prediction?
- ▶ Today, many have "abandon[ed] testing altogether"

# International trade theory

- A dominant view is that international trade is an applied branch of general-equilibrium theory
- $\blacktriangleright$  Any GE model has preferences + technology + equilibrium
- ▶ International trade theory focuses on locations, such that preferences (rarely) and technology (typically) are location-specific
- Trade theory traditionally has "international" goods markets and "domestic" factor markets
- Consumers have preferences over goods; factors are employed to produce goods
- Questions: How does international integration affect the goods market, the factor market, and welfare?
- One flavor of spatial economics is trade in goods plus mobile factors.

# Variants of trade models

One view: "positive trade theory uses a variety of models, each one suited to a limited but still important range of questions" (Jones and Neary 1980)

	Demand	Supply	Market structure
Goods markets	General; CES preferences; Translog, NHCES, etc	Constant returns to scale; Increasing returns	Perfect competition; Monopolistic competition; Oligopoly
Factor markets	Demand derived from supply of goods	Often perfectly inelastic	Almost always competitive

If you stop at the goods market, it's partial-equilibrium.

## Neoclassical trade models

- "Neoclassical trade models" are characterized by three key assumptions:
  - ▶ perfect competition
  - constant returns to scale
  - no distortions
- Can accommodate decreasing returns to scale (DRS) using "hidden" factors in fixed supply; IRS is "new trade theory"
- Given the generality of these assumptions, there is not a wealth of results, but one can obtain two canonical insights:
  - ▶ gains from trade (Samuelson 1939)
  - ▶ law of comparative advantage (Deardorff 1980)
- By contrast, we are going to dive deeply into one very specific neoclassical model

# The CES Armington model

Features:

- ▶ Concise: A one-elasticity model
- Relevant: Same macro-level predictions as other, important gravity-based models

Shortcomings:

- ▶ Supply side (endowment economy) is wholly uninteresting
- ▶ Preferences (national differentiation with IIA) are ad hoc We will discuss
  - ► Primitives
  - ▶ Existence and uniqueness of equilibrium
  - ► Solving for equilibrium
  - Computing counterfactual outcomes

## Armington model with CES preferces

- Each country has its own "signature" good (others have zero productivity in this good; maximal absolute advantage)
- Consumers in each country have identical CES preferences over the N goods with elasticity  $\sigma$  (see Dingel 2009 for CES refresher)
- ▶ Bilateral trade costs of the iceberg form  $\tau_{ij}$
- ▶ Demand: Consumer in j with total expenditure  $X_j$  spends  $X_{ij}$  on good from i

$$X_{ij} = \frac{(p_i \tau_{ij})^{1-\sigma}}{\sum_{\ell} (p_{\ell} \tau_{\ell j})^{1-\sigma}} X_j = \frac{(p_i \tau_{ij})^{1-\sigma}}{P_j^{1-\sigma}} X_j$$

Economy *i* endowed with  $Q_i$  units so GDP is  $Y_i = p_i Q_i$ 

$$X_{ij} = \frac{Y_i^{1-\sigma}}{Q_i^{1-\sigma}} \frac{X_j}{P_j^{1-\sigma}} \tau_{ij}^{1-\sigma}$$

▶ Balanced-trade equilibrium is  $\{Y_i\}_{i=1}^N$  such that

$$X_i = Y_i = \sum_j X_{ij}$$
ingel – Topics in Trade – Week 1 – 14

#### Equilibrium system of equations

Combine the last two equations to get N equations in N unknowns:

$$Y_i = \sum_j X_{ij}$$
$$= \sum_j \frac{Y_i^{1-\sigma}}{Q_i^{1-\sigma}} \frac{Y_j}{P_j^{1-\sigma}} \tau_{ij}^{1-\sigma}$$
$$= \sum_j \frac{Y_i^{1-\sigma}}{Q_i^{1-\sigma}} \frac{Y_j}{\sum_\ell (\tau_{\ell j} Y_\ell / Q_\ell)^{1-\sigma}} \tau_{ij}^{1-\sigma}$$

The N unknowns can be  $\{Y_i\}_{i=1}^N$  or  $\{p_i\}_{i=1}^N$ :

$$p_i Q_i = \sum_j p_i^{1-\sigma} \frac{p_j Q_j}{\sum_{\ell} \left( p_\ell \tau_{\ell j} \right)^{1-\sigma}} \tau_{ij}^{1-\sigma}$$

Denote "trade elasticity" by  $\epsilon \equiv \sigma - 1$  and expenditure shares by  $\lambda_{ij}$ 

$$p_i Q_i = \sum_j \underbrace{\frac{p_i^{-\epsilon} \tau_{ij}^{-\epsilon}}{\sum_{\ell} (p_{\ell} \tau_{\ell j})^{-\epsilon}}}_{\equiv \lambda_{ij}} p_j Q_j$$
  
Dingel – Topics in Trade – Week 1 – 15

### Existence and uniqueness

- ▶ We want an equilibrium to exist: a model without an equilibrium leaves us little to analyze
- ▶ Should we want the equilibrium to be unique?
  - Certainly relevant for computing outcomes
  - May be relevant to identification (Lewbel 2019), but point identification concerns uniqueness of parameters given observable outcomes, not uniqueness of outcomes
  - May be relevant for counterfactual scenarios, but we can report sets of counterfactual equilibria (multiplicity seems more a threat to forecasting than counterfactual scenarios)
- Allen, Arkolakis, Takahashi (2020) show
  - ▶  $\sigma \neq 0$ : an interior equilibrium exists
  - ▶  $\sigma \ge 0$ : all equilibria are interior
  - $\sigma \geq 1$ : interior eqlbm is unique (aggregate demand slopes down)

Recent related lit: Ouazad (2024) and Garg (2025) on enumerating all equilibria via polynomial roots; maybe check out HomotopyContinuation.jl

# Solving for equilibrium numerically (1/2)

You want to find a fixed point  $\{Y_i\}_{i=1}^N$  that satisfies

$$Y_i = \sum_j \frac{\left(Y_i/Q_i\right)^{-\epsilon} \tau_{ij}^{-\epsilon}}{\sum_{\ell} \left(Y_\ell \tau_{\ell j}/Q_\ell\right)^{-\epsilon}} Y_j.$$

Choose a numeraire to pin this down.

You might define a differentiable objective function and find its minimum (the fixed point where it is zero). This can be slow.

$$\min_{\{Y_i\}_{i=1}^N} \left(Y_i - \sum_j \frac{\left(Y_i/Q_i\right)^{-\epsilon} \tau_{ij}^{-\epsilon}}{\sum_{\ell} \left(Y_\ell \tau_{\ell j}/Q_\ell\right)^{-\epsilon}} Y_j\right)^2$$

An iterative approach can be quite fast. Function iteration means

- Guess  $\{Y_i^s\}_{i=1}^N$  starting with s = 0.
- Compute implied LHS when using  $\{Y_i^s\}_{i=1}^N$  in RHS
- Update  $\mathbf{Y}^{s+1}$  based on convex combination of  $\mathbf{Y}^s$  and implied  $\mathbf{Y}$

• Iterate until 
$$\mathbf{Y}^{s+1} = \mathbf{Y}^s$$

# Solving for equilibrium numerically (2/2)

As in Alvarez and Lucas (2007), define the excess demand function

$$f_i(\mathbf{p}) = \frac{1}{p_i} \sum_j \lambda_{ij} p_j Q_j - Q_i = \frac{1}{p_i} \sum_j \frac{(p_i \tau_{ij})^{-\epsilon}}{\sum_\ell (p_\ell \tau_{\ell j})^{-\epsilon}} p_j Q_j - Q_i$$

Compute equilibrium by defining mapping with damper  $\kappa \in (0, 1]$ :

$$M_i(\mathbf{p}) = p_i \left[1 + \kappa f_i(\mathbf{p})/Q_i\right]$$

If we start with prices such that  $\sum_{i=1}^{N} p_i Q_i = 1$ , then

$$\sum_{i} M_{i}(\mathbf{p})Q_{i} = \sum_{i} p_{i}Q_{i} + \sum_{i} p_{i}\kappa f_{i}(\mathbf{p}) = 1 + \kappa \sum_{i} p_{i} \left[ \frac{1}{p_{i}} \sum_{j} \lambda_{ij}p_{j}Q_{j} - Q_{i} \right]$$
$$= 1 + \kappa \sum_{i} \sum_{j} \lambda_{ij}p_{j}Q_{j} - \kappa \sum_{i} p_{i}Q_{i} = 1$$

This maps the set  $\{\mathbf{p} \in \mathbb{R}^N_+ : \sum_i p_i Q_i = 1\}$  to itself. Iteration converges to  $M_i(\mathbf{p}) = p_i$  (see Alvarez and Lucas 2007).

Dingel - Topics in Trade - Week 1 - 18

#### Introducing a production function

Switch from an endowment economy to a simple production function

- One factor of production in fixed supply:  $L_i$
- Constant returns to scale:  $Q_i = A_i L_i$
- ▶ Perfect competition:  $p_i = w_i/A_i$  and  $Y_i = w_iL_i$
- (Choose units to define  $T_i \equiv A_i^{\epsilon}$ )

Our equilibrium system of equations is now

$$w_i L_i = \sum_j \frac{T_i (w_i \tau_{ij})^{-\epsilon}}{\sum_{\ell} T_\ell (w_\ell \tau_{\ell j})^{-\epsilon}} w_j L_j$$

# Introducing asymmetric preferences

Consider an Armington model with asymmetric preferences:

$$U_{j} = \left(\sum_{i} \beta_{ij} q_{ij}^{(\sigma-1)/\sigma}\right)^{\sigma/(\sigma-1)}$$
$$\Rightarrow \frac{X_{ij}}{X_{j}} = \beta_{ij} \left(\frac{p_{ij}}{P_{j}}\right)^{1-\sigma} = \frac{w_{i}^{1-\sigma}}{P_{j}^{1-\sigma}} \beta_{ij} \tau_{ij}^{1-\sigma}$$

Bilateral trade costs and bilateral preferences are observationally equivalent.

(The CES price index  $P_j$  on this slide differs from previous  $P_j$ .)

### Welfare

- There is only one factor of production and it is inelastically supplied
- If we know the CES price index, we can study the real wage  $w_i/P_i$ , real income  $w_iL_i/P_i$ , and so forth for each country

 $\blacktriangleright$  Real wage in country *j* with symmetric preferences:

$$\frac{w_j}{P_j} = \frac{w_j}{\left(\sum_{i=1}^N (p_i \tau_{ij})^{1-\sigma}\right)^{\frac{1}{1-\sigma}}} = \frac{w_j}{\left(\sum_{i=1}^N (w_i \tau_{ij}/A_i)^{1-\sigma}\right)^{\frac{1}{1-\sigma}}}$$

# Counterfactual outcomes

Counterfactual scenarios:

- If our model has parameters  $\{T_i, L_i, \tau_{ij}, \epsilon\}$ , a counterfactual scenario is an alternative parameter vector  $\{T'_i, L'_i, \tau'_{ij}, \epsilon'\}$ .
- ► The model's baseline equilibrium outcomes are {w<sub>i</sub>} and the counterfactual outcomes by primes are {w'<sub>i</sub>}

(Be careful with  $\epsilon \to \epsilon'$  exercises)

We can address many counterfactuals even in this simple model. Examples:

- ▶ How large are the gains from trade relative to autarky?
- ▶ How much would countries gain from frictionless trade?
- ▶ Which countries gain from Chinese productivity growth?
- ▶ When is productivity growth immiserizing?

# Counterfactual outcomes by exact hat algebra

One way of stating counterfactual outcomes is "exact hat algebra" (Costinot and Rodriguez-Clare 2014)

- A counterfactual equilibrium can be expressed in terms of counterfactual endogenous outcomes relative to baseline endogenous outcomes, counterfactual exogenous parameters relative to baseline exogenous parameters, elasticities, and baseline equilibrium shares.
- ► The name refers to the "hat algebra" of Jones (1965): obtaining comparative statics by totally differentiating a model in logarithms
- It's "exact" because it's global (not only small changes) thanks to knowing the whole demand and supply system
- ▶ We will discuss the use (and misuse) of this technique (and its name) more later in the course

# Counterfactual Armington outcomes by EHA (1/2)

Start from the market-clearing condition and the gravity equation:

$$w_i L_i = \sum_{j=1}^N \lambda_{ij} w_j L_j \qquad \lambda_{ij} = \frac{T_i \left(\tau_{ij} w_i\right)^{-\epsilon}}{\sum_{l=1}^N T_l \left(\tau_{lj} w_l\right)^{-\epsilon}}$$

We consider a shock to  $\hat{T}_i \equiv \frac{T'_i}{T_i}$ . By assumption,  $\hat{\tau} = 1$  and  $\hat{L} = 1$ . We want to solve for the endogenous variables  $\hat{\lambda}_{ij}, \hat{X}_{ij}$  and  $\hat{w}_i$ . In the following derivation, define "sales shares" by  $\gamma_{ij} \equiv \frac{X_{ij}}{Y_i}$ .

$$w_{i}L_{i} = \sum_{j=1}^{N} \lambda_{ij}w_{j}L_{j}, \quad w_{i}'L_{i}' = \sum_{j=1}^{N} \lambda_{ij}'w_{j}'L_{j} = \sum_{j=1}^{N} X_{ij}'$$
$$\hat{w}_{i}\hat{L}_{i} = \sum_{j=1}^{N} \frac{X_{ij}'}{w_{i}L_{i}} = \sum_{j=1}^{N} \frac{X_{ij}}{w_{i}L_{i}}\hat{X}_{ij} \equiv \sum_{j=1}^{N} \gamma_{ij}\hat{X}_{ij}$$
(1)

# Counterfactual Armington outcomes by EHA (2/2)

$$\lambda_{ij} = \frac{T_i (\tau_{ij} w_i)^{-\epsilon}}{\sum_{l=1}^N T_l (\tau_{lj} w_l)^{-\epsilon}}, \quad \lambda'_{ij} = \frac{T'_i (\tau_{ij} w'_i)^{-\epsilon}}{\sum_{l=1}^N T'_l (\tau_{lj} w'_l)^{-\epsilon}}$$
$$\hat{\lambda}_{ij} \equiv \frac{\lambda'_{ij}}{\lambda_{ij}} = \hat{T}_i \hat{w}_i^{-\epsilon} \hat{\tau}_{ij}^{-\epsilon} \frac{\sum_{l=1}^N T_l (\tau_{lj} w_l)^{-\epsilon}}{\sum_{l=1}^N T'_l (\tau_{lj} w'_l)^{-\epsilon}} = \frac{\hat{T}_i \hat{w}_i^{-\epsilon} \hat{\tau}_{ij}^{-\epsilon}}{\sum_{l=1}^N \lambda_{lj} \hat{T}_l \hat{w}_l^{-\epsilon} \hat{\tau}_{lj}^{-\epsilon}} \quad (2)$$

Combining equations (1) and (2) under the assumptions that  $\hat{Y}_i = \hat{X}_i$ and  $\hat{\tau} = \hat{L} = 1$ , we obtain a system of equation characterizing an equilibrium  $\hat{w}_i$  as a function of shocks  $\hat{T}_i$ , initial equilibrium shares  $\lambda_{ij}$  and  $\gamma_{ij}$ , and the trade elasticity  $\epsilon$ :

$$\hat{w}_i \hat{L}_i = \sum_{j=1}^N \gamma_{ij} \hat{X}_{ij} = \sum_{j=1}^N \gamma_{ij} \hat{\lambda}_{ij} \hat{w}_j \Rightarrow \hat{w}_i = \sum_{j=1}^N \frac{\gamma_{ij} \hat{T}_i \hat{w}_i^{-\epsilon} \hat{w}_j}{\sum_{l=1}^N \lambda_{lj} \hat{T}_l \hat{w}_l^{-\epsilon}}$$

Given a model parameterization that defines  $\epsilon, \lambda_{ij}$ , and  $\gamma_{ij}$ , we can choose arbitrary productivity shocks  $\{\hat{T}_i\}_{i=1}^N$  and solve for  $\{\hat{w}\}_{i=1}^N$ . (This generalizes to arbitrary  $\hat{\tau}, \hat{L}$ .)

Dingel - Topics in Trade - Week 1 - 25

## Counterfactual outcomes: Autarky and free trade

Autarky

► The autarky counterfactual scenario is the alternative parameter vector in which  $\tau_{ij} = \infty$   $i \neq j$  ( $\{T_i, L_i, \{\tau_{ij}^{-1}\} = I_N, \epsilon\}$ )

► Can compute by exact hat algebra:  $\hat{\tau}_{ij} = \infty$  for  $i \neq j$ Free trade

- Given  $\{T_i, L_i, \tau_{ij}, \epsilon\}$  where  $\tau_{ii} = 1 \forall i$ , the free-trade counterfactual scenario is the alternative parameter vector in which  $\tau_{ij} = 1 \forall ij (\{T_i, L_i, \mathbf{1}_{N \times N}, \epsilon\})$
- Cannot compute using only shares. Need level of  $\tau_{ij}$ .

#### Special case: Symmetric trade costs

When  $\tau_{ij} = \tau_{ji} \forall i, j$ , we can rewrite the system in terms of market access  $\Phi_i \equiv P_j^{1-\sigma}$  (see Appendix A.1.3 of Dingel, Meng, Hsiang):

$$Y_{i} = w_{i}L_{i} = \sum_{j} \left(\frac{w_{i}}{A_{i}}\right)^{-\epsilon} \tau_{ij}^{-\epsilon} \frac{w_{j}L_{j}}{\Phi_{j}} = \left(\frac{w_{i}}{A_{i}}\right)^{-\epsilon} \Omega_{i}$$

$$\Rightarrow \frac{w_{i}}{A_{i}} = \left(\frac{\Omega_{i}}{A_{i}L_{i}}\right)^{\frac{1}{\epsilon+1}}$$

$$\Rightarrow \Phi_{i} = \sum_{j} \tau_{ji}^{-\epsilon} \left(\frac{w_{j}}{A_{j}}\right)^{-\epsilon} = \sum_{j} \tau_{ji}^{-\epsilon} \left(A_{j}L_{j}/\Omega_{j}\right)^{\frac{\epsilon}{\epsilon+1}}$$

$$= \sum_{j} \tau_{ji}^{-\epsilon} \left(A_{j}L_{j}/\Phi_{j}\right)^{\frac{\epsilon}{\epsilon+1}}$$

The last equality exploits the fact that we can normalize incomes such that  $\Phi_i = \Omega_i$  when trade is balanced and  $\tau_{ij}^{-\epsilon}$  is symmetric (Anderson and van Wincoop 2003; Head and Mayer 2014).

#### Multi-sector Armington model

▶ **Preferences**. Cobb-Douglas over sectors s = 1, ..., S and CES within:

$$P_i = \prod_{s=1}^{S} P_{is}^{\alpha_{is}}$$
 and  $P_{is} = \left(\sum_{i=1}^{N} p_i(\omega_s)^{1-\sigma_s}\right)^{1/(1-\sigma_s)}$ 

- ▶ **Production**. Sector-specific productivities  $A_{is}$  and trade costs  $\tau_{ijs}$ .
- Gravity equation. Denote sales from *i* to *j* in sector *s* by  $X_{ijs}$  and *j*'s total expenditure by  $X_j \equiv \sum_{i=1}^N \sum_{s=1}^S X_{ijs}$ .

$$\lambda_{ijs} = \frac{X_{ijs}}{X_{js}} = \frac{T_{is} \left(\tau_{ijs} w_i\right)^{-\epsilon_s}}{\sum_{l=1}^{N} T_{ls} \left(\tau_{ljs} w_l\right)^{-\epsilon_s}} = \frac{T_{is} \left(\tau_{ijs} w_i\right)^{-\epsilon_s}}{\Phi_{js}}$$

• Equilibrium. Labor-market clearing, goods-market clearing, and budget constraints mean total income  $Y_i = w_i L_i$  and sectoral income  $Y_{is} = w_i L_{is}$  satisfy  $Y_{is} = \sum_{j=1}^{N} X_{ijs}$ ,  $Y_i = \sum_{s=1}^{S} Y_{is}$ , and  $X_{is} = \alpha_{is} Y_i$ for all countries.

$$Y_{is} = \sum_{j=1}^{N} \lambda_{ijs} \alpha_{js} \sum_{s'=1}^{S} Y_{js'}.$$

(Recall  $T_{is} = A_{is}^{\epsilon_s} = A_{is}^{\sigma_1 - 1}$ )

Dingel - Topics in Trade - Week 1 - 28



Next week: Gravity regressions

Extra time? Discuss assignment 4

Dingel - Topics in Trade - Week 1 - 29