Lecture 15

Travel cost and recreation demand

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AEM 4510

Roadmap

- How do we estimate the value of recreational goods?

Background

Should we separate the Great Lakes and Mississippi?

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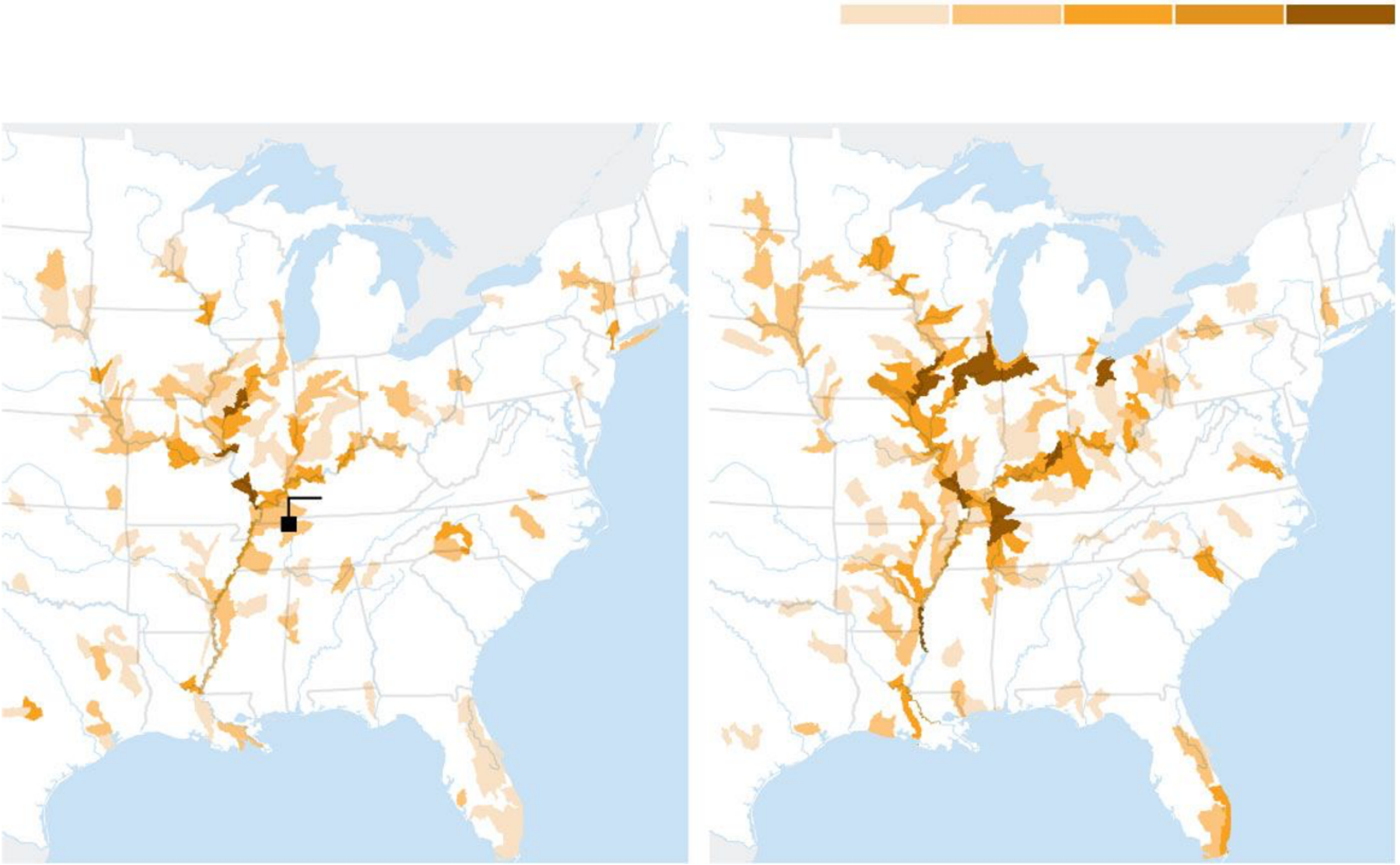

Should we separate the Great Lakes and Mississippi?

The Great Lakes

Carpe diem

Some are worried that Asian carp are poised to invade Lake Michigan

Jul 28th 2012 | From the print edition

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WHEN Eric Gittinger, a biologist, goes to work on the Illinois and Mississippi Rivers, he has to look out. The Asian carp that are swimming up from the South, where they escaped from fish farms decades ago, can leap 10 feet in the air or torpedo themselves twice that distance across the water. Larger fish can weigh 40lb (18kg), and Mr Gittinger gets regularly whacked by them.

Yet what most worries people about Asian carp (in fact, several different invasive carp species) is the fact that they are outeating native fish in the rivers, and now seem poised to invade the Great Lakes. This could harm the $7 billion sport-fishing industry, and damage the ecosystem of the largest body of fresh water in the world.

In 2002 the Army Corps of Engineers (ACE) installed a series of electric barriers 37 miles downriver in the Chicago Sanitary and Ship Canal, an artificial channel that links the lakes with the Mississippi and its tributaries. But people fear they may not be working. Recently, multiple traces of Asian-carp DNA have been found in Chicago's Lake Calumet—far beyond the electric fence (see map), and a stone's throw from Lake Michigan.

Should we separate the Great Lakes and Mississippi?

Benefits from barriers accrue to anglers in the Great Lakes, both commercial and recreational

Costs come from cost of building the barriers plus cost of maintaining them, plus costs of reduced shipping (if any), plus any other costs associated with the barriers

How do we figure out the benefits from recreational anglers?

Why do we need travel cost?

Recreational areas have value

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Recreational areas **have value**

Their quality also has value

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If someone dumped toxic waste in Taughannock does that have zero cost?

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This gives us a demand curve for sites/amenities, so we can value changes in these environmental amenities

Hotelling

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Harold Hotelling proposed the first indirect method for measuring the demand of a non-market good in 1947

Hotelling

> Let concentric zones be defined around each park so that the cost of travel to the park from all points in one of these zones is approximately constant. The persons entering the park in a year, or a suitable chosen sample of them, are to be listed according to the zone from which they came. The fact that they come means that the service of the park is at least worth the cost, and this cost can probably be estimated with fair accuracy.

Hotelling

> A comparison of the cost of coming from a zone with the number of people who do come from it, together with a count of the population of the zone, enables us to plot one point for each zone on a demand curve for the service of the park. By a judicious process of fitting, it should be possible to get a good enough approximation to this demand curve to provide, through integration, a measure of consumers' surplus..

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About twelve years after, Trice and Wood (1958) and Clawson (1959) independently implemented the methodology

Theoretical foundation

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Consider a single consumer and a single recreation site

The consumer has:

- Total number of recreation trips: x, to site of quality: q
- Total budget of time: T
- Working time: H
- Non-recreation, non-work time: l
- Hourly wage: w
- Money cost of reaching the site: c

Theoretical foundation

This lets us write down the consumer's utility maximization problem:

$$\max_{x,z,l} U(x,z,l,q) \quad \text{subject to:} \quad \underbrace{wH = cx + z}_{\text{money budget}},\ \underbrace{T = H + l + tx}_{\text{time budget}}$$

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Combine the two constraints to get:

$$\max_{x,z,l} U(x,z,l,q) \quad \text{subject to:} \quad \underbrace{wT = z + (c + wt)x + wl}_{\text{combined money/time budget}}$$

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$$\max_{x,z,l} U(x, z, l, q) \quad \text{subject to:} \quad \underbrace{Y = z + px + wl}_{\text{combined budget}}$$

Solve the constraint for z and substitute into the utility function...

Theoretical foundation

$$\max_{x,l} U\left(x, Y - px - wl, l, q\right)$$

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$$\max_{x,l} U\left(x, Y - px - wl, l, q\right)$$

This has first-order conditions:

$$[x]\ \ U_x - pU_z = 0 \rightarrow \frac{U_x}{U_z} = p$$

and

$$[l]\ \ -wU_z + U_l = 0 \rightarrow \frac{U_l}{U_z} = w$$

Theoretical foundation

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What does this mean?

The value of the recreational trip to the consumer, in dollar terms, is revealed by the full price p

Theoretical foundation

$$U_x - pU_z = 0 \qquad -wU_z + U_l = 0$$

The above FOCs are two equations, the consumer had two choices (x,l) so we had two unknowns

We can thus solve for x (and l) as a function of the parameters (p,Y,q):

$$x = f(p, Y, q)$$

This is simply the consumer's **demand curves** for recreation as a function of the full price p, full budget Y, and quality q

Theoretical foundation

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Once we have it, we can compute surplus!

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  - Travel costs from all points within each zone to the site are sufficiently close in magnitude to justify neglecting the differences

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  - Travel costs from all points within each zone to the site are sufficiently close in magnitude to justify neglecting the differences
- From a sample of visitors (v_i) at the recreation site, determine zones of origin and their populations (n_i)
- Calculate the per capita visitation rates for each zone of origin $(t_i = (v_i/n_i))$

Zonal (single-site) model

- Construct a travel cost measure (tc_i) that reflects the round-trip costs of travel from the zone of origin to the recreation site (time and gas), + an entry fee (fee) which may be zero and does not vary across zones

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- Use statistical methods to estimate the trip demand curve: the relationship between per-capita visitation rates, cost per visit, [and travel costs to other sites (tc_{si})] controlling for socioeconomic differences

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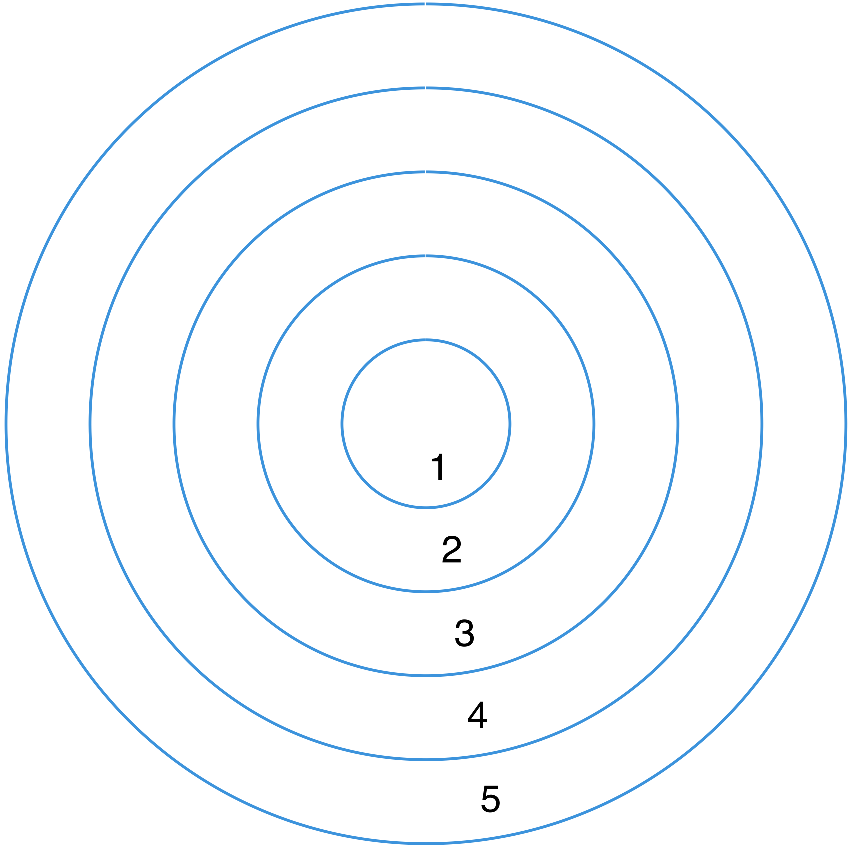
- Use statistical methods to estimate the trip demand curve: the relationship between per-capita visitation rates, cost per visit, [and travel costs to other sites (tc_{si})] controlling for socioeconomic differences

- $t_i = g(tc_i + fee; tc_{si}, x_i) + \varepsilon_i$ where g can be linear

Zonal (single-site) model

Here's a simple example of a set of zones 1-5:



Zonal (single-site) model

Suppose we have the following data:

```
## # A tibble: 5 × 5
##   zone   dist   pop  cost   vpp
##   <chr> <dbl> <dbl> <dbl> <dbl>
## 1 A         2 10000    20    15
## 2 B        30 10000    30    13
## 3 C        90 20000    65     6
## 4 D       140 10000    80     3
## 5 E       150 10000    90     1
```

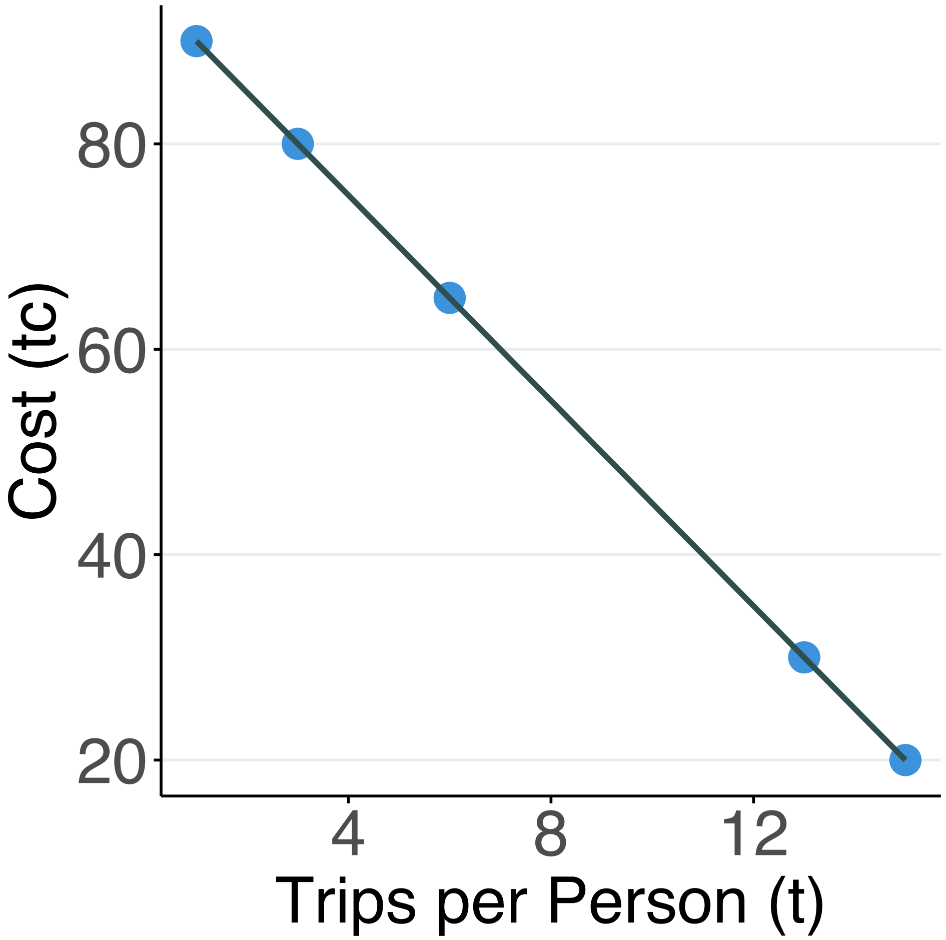
If we plot cost by visits per person, we have a measure of the demand curve...

Zonal (single-site) model

This is a very simple example where it happens to be an exactly straight line, most likely the data won't be this perfect

The line is simply from estimating:

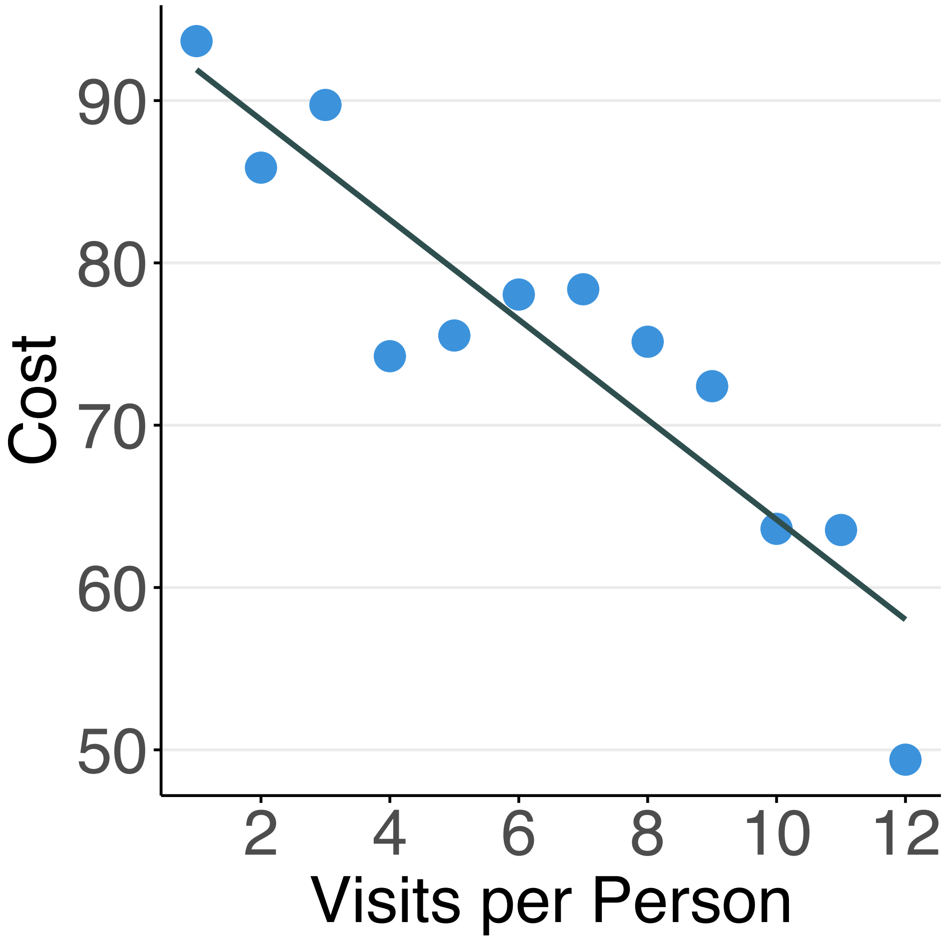
$$t_i = \beta_0 + \beta_1 tc_i + \varepsilon_i$$



Zonal (single-site) model

The data will most likely look like this, but even this is probably too clean

It ignores things like income, other sites, other household characteristics



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Entry fee on the y-axis (price), and the number of predicted total visits on the x-axis (quantity)

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The (use) value of the park/site to each zone is given by the area underneath the corresponding demand curve

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What is the right functional form for demand?

How do we measure the opportunity cost of time?

How do we treat multi-purpose trips?

How do we value particular site attributes? Can't disentangle them at a single site

Multi-site model

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What is the benefit of water clarity?

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What is the benefit of a fish restocking program?

- Need to know the value of fish catch rate for visitors

What is the benefit of water clarity?

What is the benefit of tree replanting?

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The multi-site model works as follows

Multi-site model

Step 1: Do the single-site estimation for each site:

$$T_{ij} = \beta_{0j} + \beta_{1j} tc_{ij} + \beta_{2j} tc_{sij} + \beta_{3j} x_i + \varepsilon_{ij}$$

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These βs tell us the slope (β_{1j}) and intercept ($\beta_{0j}, \beta_{2j}, \beta_{3j}$)

β_{2j}, β_{3j} capture how the cost of substitute sites and household characteristics shift demand up and down

Multi-site model

Step 3: Take each set of J coefficient estimates and use them as the dependent variable in a regression on site attributes z:

$$\hat{\beta}_{0j} = \alpha_{00} + \alpha_{01} z_j + \epsilon_{0j}$$

$$\hat{\beta}_{1j} = \alpha_{10} + \alpha_{11} z_j + \epsilon_{1j}$$

$$\hat{\beta}_{2j} = \alpha_{20} + \alpha_{21} z_j + \epsilon_{2j}$$

$$\hat{\beta}_{3j} = \alpha_{30} + \alpha_{31} z_j + \epsilon_{3j}$$

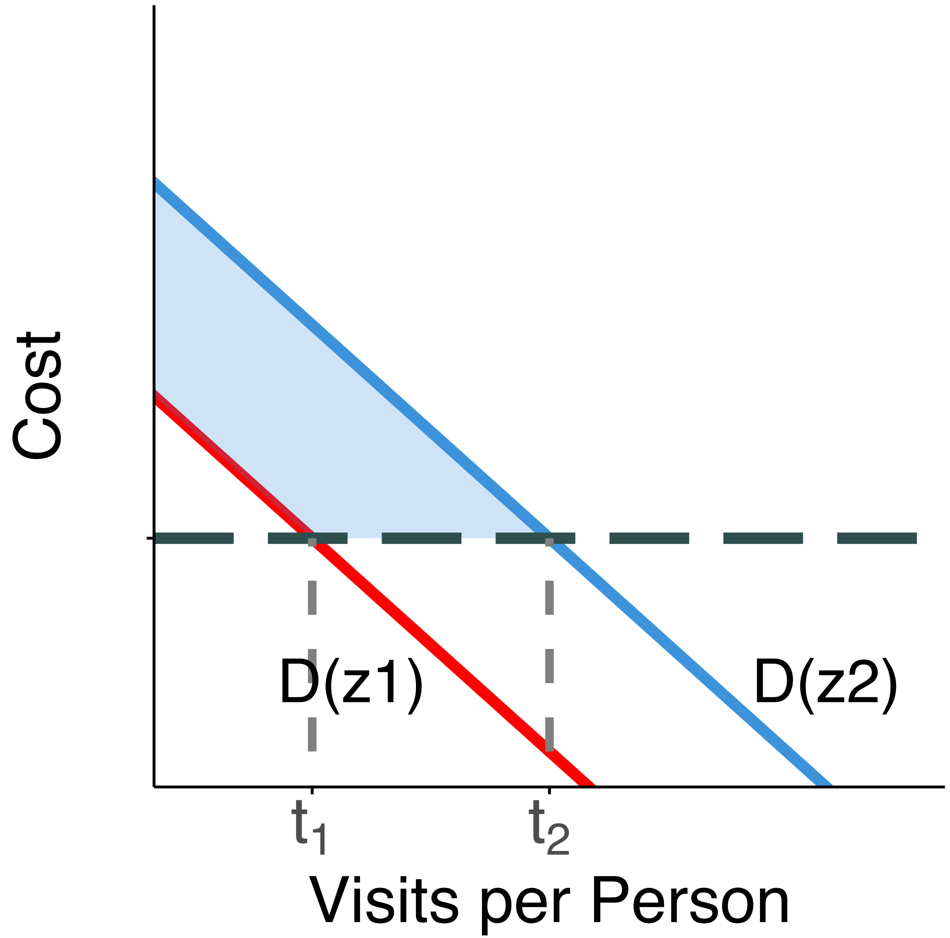
The $\alpha_{\times 1}$ coefficients tell us how the demand curve shifts $(\alpha_{00}, \alpha_{02}, \alpha_{03})$ or rotates (α_{01}) as we change z

Valuing attributes with a multi-site model

If we improve the quality of a site from z_1 to z_2, demand for that site shifts up

The gain in CS, holding the cost fixed, is given by the blue area

Once we estimate demand curves, we can see how welfare changes when we alter quality characteristics!



Multi-site example

```
trip_data <- read_csv("data/trip_data.csv")
```

```
## Rows: 2600 Columns: 7

## ── Column specification ────────────────────────────────────────────────────────
## Delimiter: ","
## dbl (7): house_num, site, trips, income, travel_cost, travel_cost_other, wat...

##
## ℹ Use `spec()` to retrieve the full column specification for this data.
## ℹ Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

```
trip_data
```

```
## # A tibble: 2,600 × 7
##    house_num  site trips income travel_cost travel_cost_other water_clarity
##        <dbl> <dbl> <dbl>  <dbl>       <dbl>             <dbl>         <dbl>
##  1         1     1     4 40450.        38.9              16.4         0.506
##  2         2     1     5 60304.        29.8              37.5         0.506
```

First stage estimation

```r
# first stage of multi-site
site_estimates <- map_dfr(unique(trip_data$site), function(site_in){
  lm(trips ~ travel_cost + travel_cost_other + income,
     trip_data %>% filter(site == site_in)) %>%
    broom::tidy() %>%
    select(estimate) %>%
    mutate(site = site_in) %>%
    list() %>%
    tibble_row() %>%
    unlist()
}) %>%
  select(1:5) %>%
  magrittr::set_colnames(c("intercept", "own_price", "cross_price", "income", "site"))
```

First stage estimation

```
site_estimates
```

```
## # A tibble: 26 × 5
##    intercept own_price cross_price    income  site
##        <dbl>     <dbl>       <dbl>     <dbl> <dbl>
##  1     2.99   -0.0161      0.0106  0.0000321     1
##  2     2.45   -0.0117      0.0101  0.0000397     2
##  3     2.37   -0.0197      0.0111  0.0000450     3
##  4     2.33   -0.0187      0.0119  0.0000438     4
##  5     2.05   -0.0143      0.0139  0.0000450     5
##  6    -0.236  -0.00668     0.00972 0.0000321     6
##  7     2.67   -0.0210      0.0118  0.0000395     7
##  8    -0.346  -0.00395     0.00987 0.0000324     8
##  9     2.98   -0.0133      0.0107  0.0000315     9
## 10    -0.103  -0.00943     0.0105  0.0000302    10
## # … with 16 more rows
```

Take estimates, join with water clarity

```
# merge in water clarity
estimation_df <- site_estimates %>%
  left_join(trip_data %>% distinct(site, water_clarity))
```

```
## Joining, by = "site"
```

```
estimation_df
```

```
## # A tibble: 26 × 6
##    intercept own_price cross_price    income  site water_clarity
##        <dbl>     <dbl>       <dbl>     <dbl> <dbl>         <dbl>
##  1     2.99   -0.0161      0.0106  0.0000321     1         0.506
##  2     2.45   -0.0117      0.0101  0.0000397     2         0.503
##  3     2.37   -0.0197      0.0111  0.0000450     3         0.515
##  4     2.33   -0.0187      0.0119  0.0000438     4         0.515
##  5     2.05   -0.0143      0.0139  0.0000450     5         0.515
##  6    -0.236  -0.00668     0.00972 0.0000321     6         0.481
##  7     2.67   -0.0210      0.0118  0.0000395     7         0.539
##  8    -0.346  -0.00395     0.00987 0.0000324     8         0.482
```

Second stage

```
# second stage of multi-site
demand_shifts <- map_dfr(names(estimation_df)[1:4],
        function(coefficient) {
          reg_formula <- as.formula(paste0(coefficient, " ~ water_clarity"))
          lm(reg_formula, estimation_df) %>%
            broom::tidy() %>%
            mutate(coeff = coefficient) %>%
            slice(2)
        }
)
```

Second stage

```
demand_shifts
```

```
## # A tibble: 4 × 6
##   term            estimate std.error statistic      p.value coeff
##   <chr>              <dbl>     <dbl>     <dbl>        <dbl> <chr>
## 1 water_clarity 48.0      6.29           7.62 0.0000000733 intercept
## 2 water_clarity -0.171    0.0302        -5.67 0.00000770   own_price
## 3 water_clarity  0.0241   0.00867        2.78 0.0104       cross_price
## 4 water_clarity  0.000165 0.0000394      4.18 0.000330     income
```

The estimates column tells us how a change in water clarity (from 0 to 100%), shifts or rotates our demand curve