

Lecture 13

Health // Difference-in-differences

Ivan Rudik
AEM 6510

Roadmap

- How do we estimate a treatment effect when the treated and control groups do not (counterfactually) look the same in the cross-section?
- What is the mortality cost of lead?

Difference-in-differences

Our comparisons so far

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2. Comparing two groups where there is a local discontinuity (i.e. discrete change) in policy (regression discontinuity)

In both of these we are comparing groups in the **cross-section**: there is no concept of time, before and after a policy was enacted, etc

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Let's try to relax this assumption by exploiting **temporal comparisons** in addition to the cross-sectional comparison

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Difference-in-differences

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It's exactly that for an RCT since D was randomly assigned, and it's the difference in conditional expectations (conditional on being around the threshold) for RDD

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The name comes from the fact that we are taking the difference (3) between two differences (1 and 2)

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DD assumption: the treatment and control group would have followed **parallel trends** in the absence of treatment

- i.e. the difference in outcomes would have remained constant

This is much less stringent than requiring the outcomes to have been the same in the absence of treatment

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Difference-in-differences

Example: Suppose we want to understand the effect of a conservation policy passed in New York on biodiversity

Suppose also that:

- The effect of the New York policy is given by **B**
- Each state has its own fixed determinants of biodiversity (e.g. land cover, average temperature, etc) given by **NY, PA, MA, etc**
- Each period has its own determinants of biodiversity, common across all states (e.g. federal policy, global climate change) given by **T₀, T₁**, where 0 is years before the policy is passed, and 1 is after

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1. Compare New York to another state after the policy is passed
2. Compare New York to itself, before and after the policy is passed

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If we take a simple difference across states, we can't disentangle whether the difference is due to the policy **B** or differences in these other factors **NY - PA**

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If we take a simple difference over time, we can't disentangle whether the difference is due to the policy **B** or differences in other factors that are changing over time $T_1 - T_0$

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We take the time series differences for NY and PA:

	After	Before	Time Series Difference
New York	$B + NY + T_1$	$NY + T_0$	$(B + NY + T_1) - (NY + T_0) = B + T_1 - T_0$
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Next, difference the time series differences to get the DD¹

¹You can also difference in the opposite order and end up with the same result

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The cross-sectional difference lets us control for all period-specific determinants common across all states (**T₁**)

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The cross-sectional difference lets us control for all period-specific determinants common across all states (**T₁**)

Combining these two differences addresses both and lets us recover **B**, the true effect of the policy!

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It only can address determinants of biodiversity that are either:

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2. Time-varying, but common across all states

If there is a determinant of biodiversity that is varying over time, and differentially across states, DD will fail to correctly estimate **B**

- State climate trends, state pollution trends, etc

Difference-in-differences

Suppose that there is another determinant of biodiversity C^{NY}_1, C^{NY}_0 that only occurs in New York and varies over time

- e.g. climate in New York relative to Pennsylvania

Our DD is then

	After	Before	Time Series Difference
New York	$B + NY + T_1 + C^{NY}_1$	$NY + T_0 + C^{NY}_0$	$(B + NY + T_1) - (B + NY + T_1) = B + T_1 - T_0 + C^{NY}_1 - C^{NY}_0$
Pennsylvania	$PA + T_1$	$PA + T_0$	$(PA + T_1) - (PA + T_0) = T_1 - T_0$
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DD cannot isolate the effect of B versus $C^{NY}_1 - C^{NY}_0$

There cannot be any (uncontrolled for) time varying differences between NY and PA if we want to correctly estimate B

Difference-in-differences: to the data

Now lets see how this works in practice: [notebook here](#)

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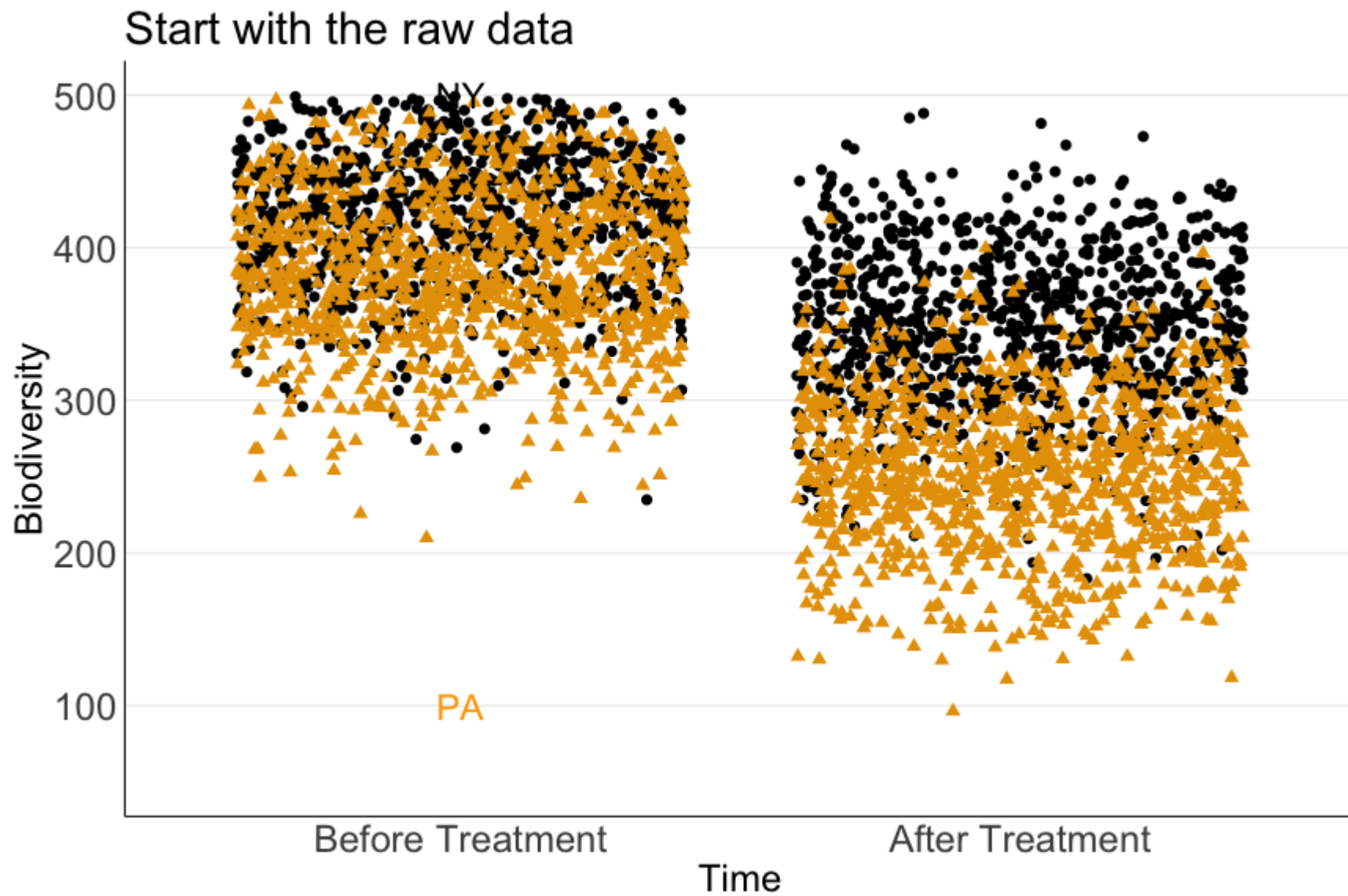
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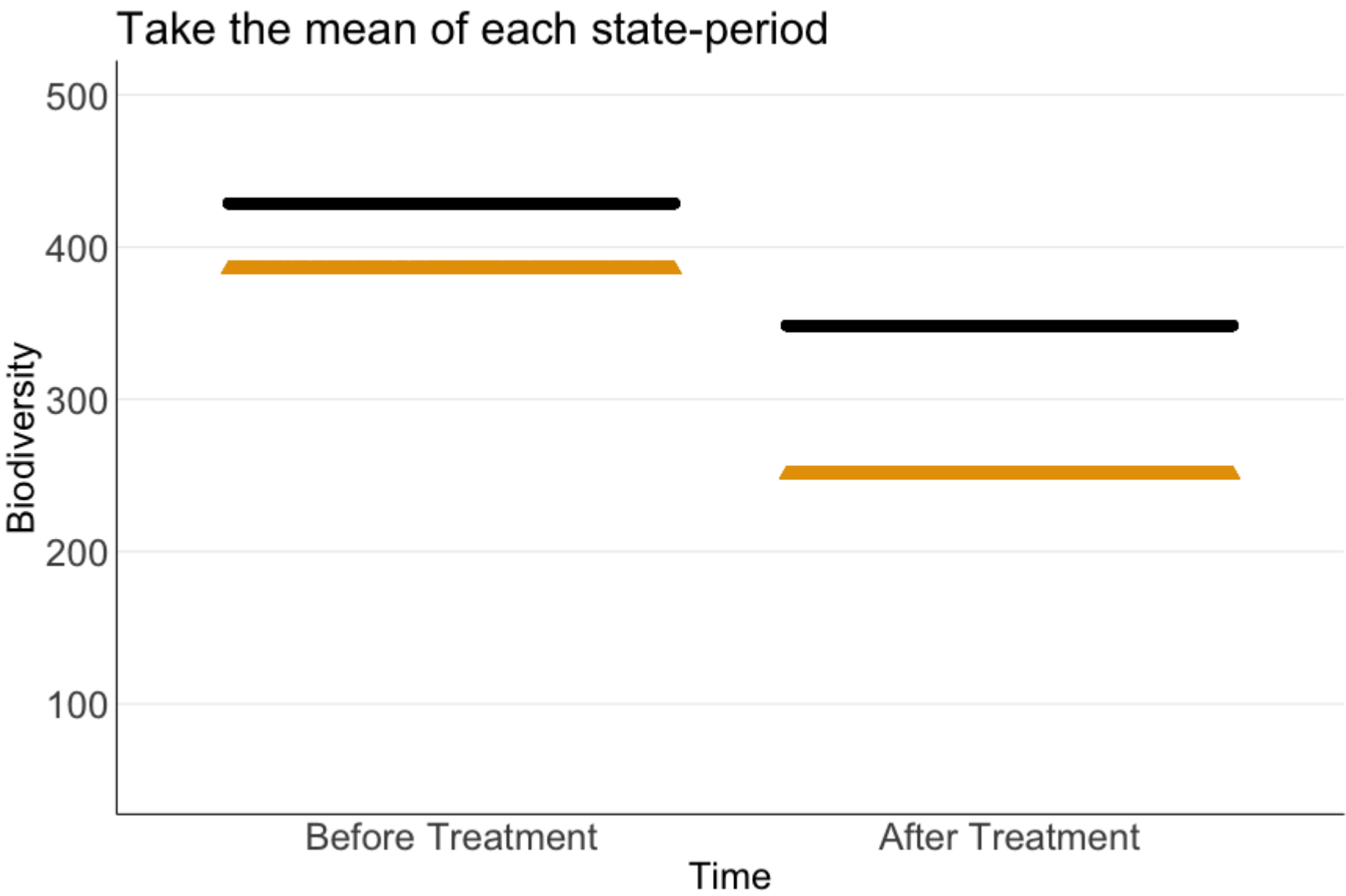
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This is a good skill to practice to make sure you understand methods and that your code works correctly

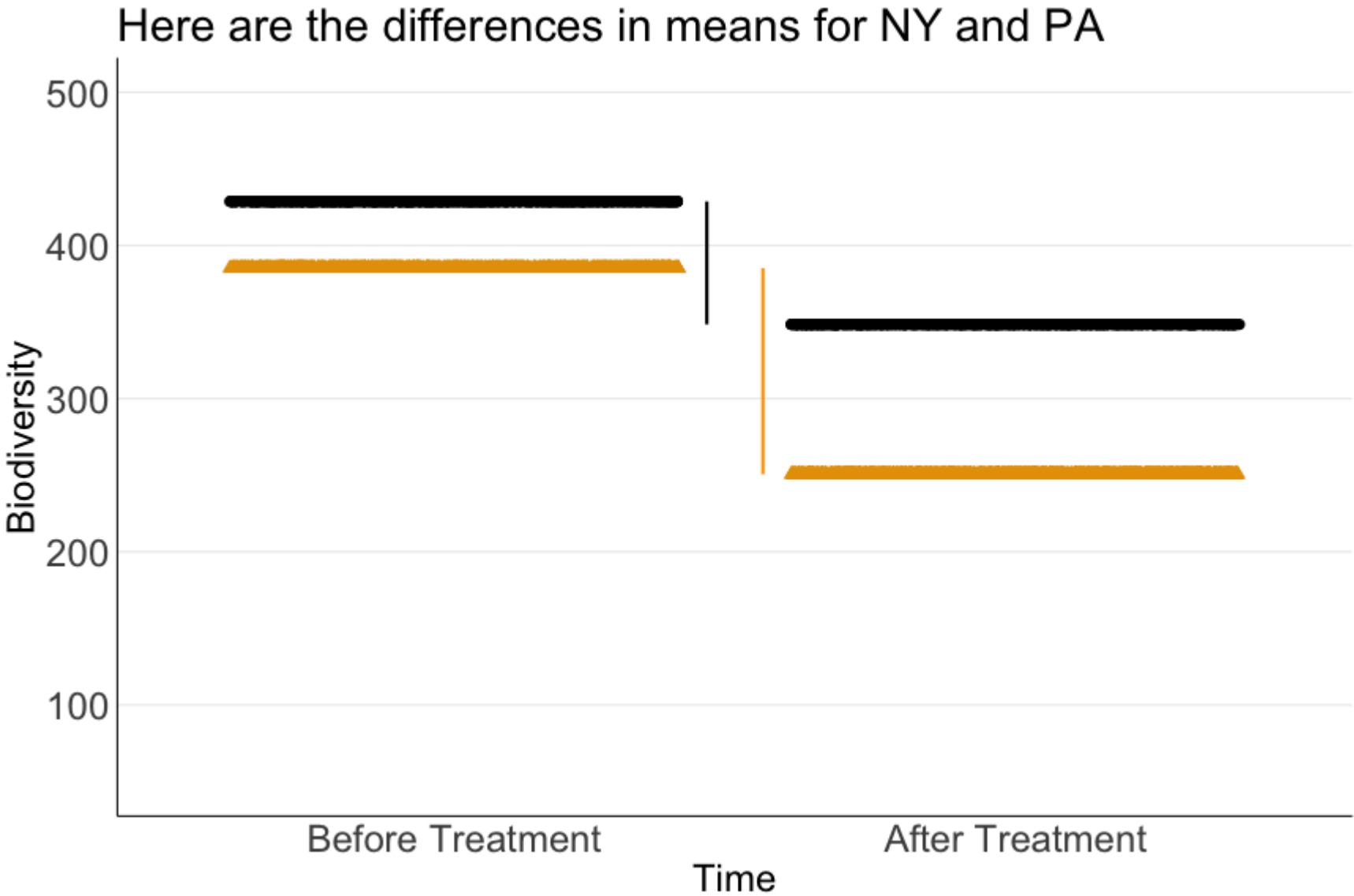
DD step 1



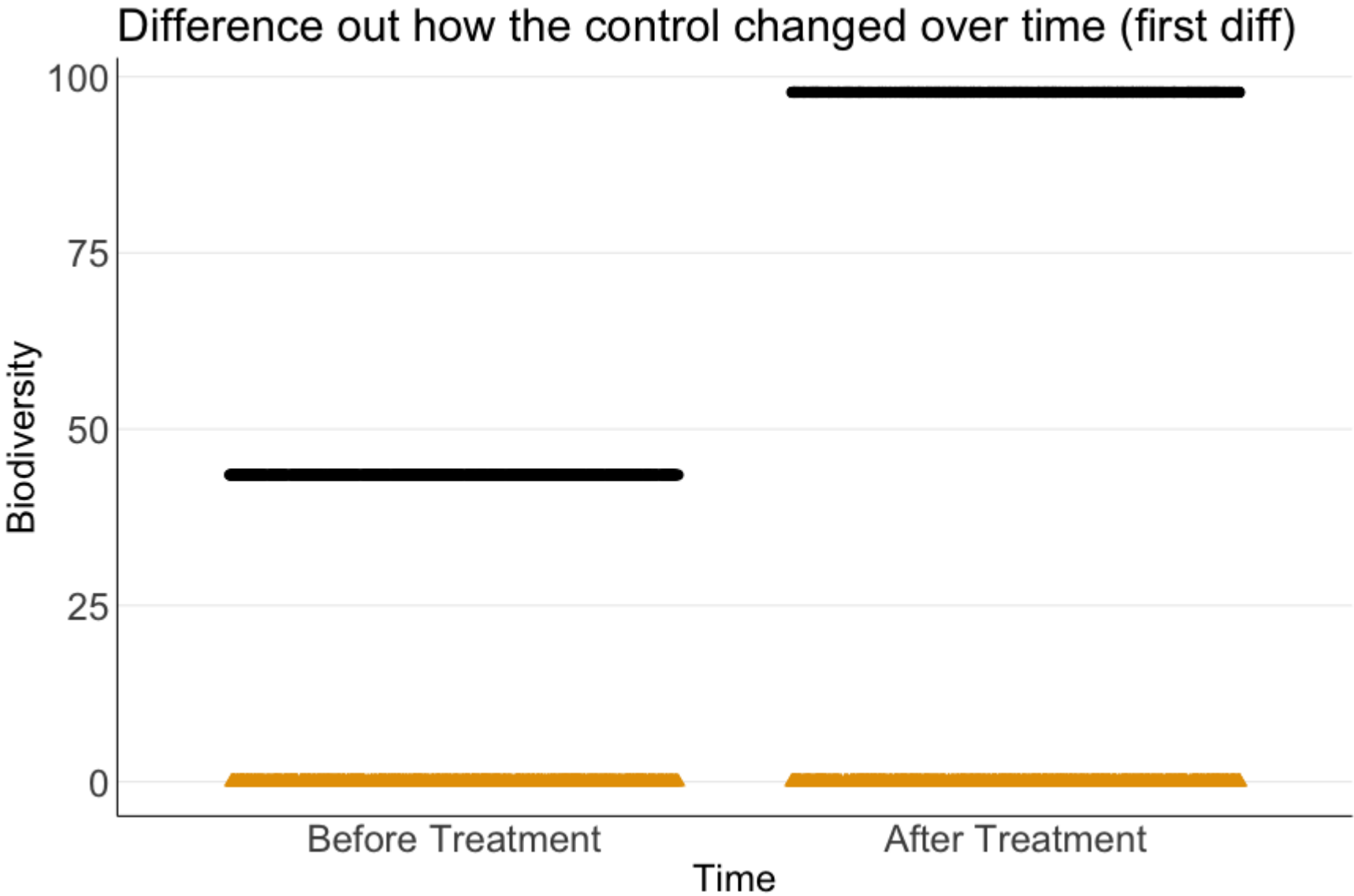
DD step 2



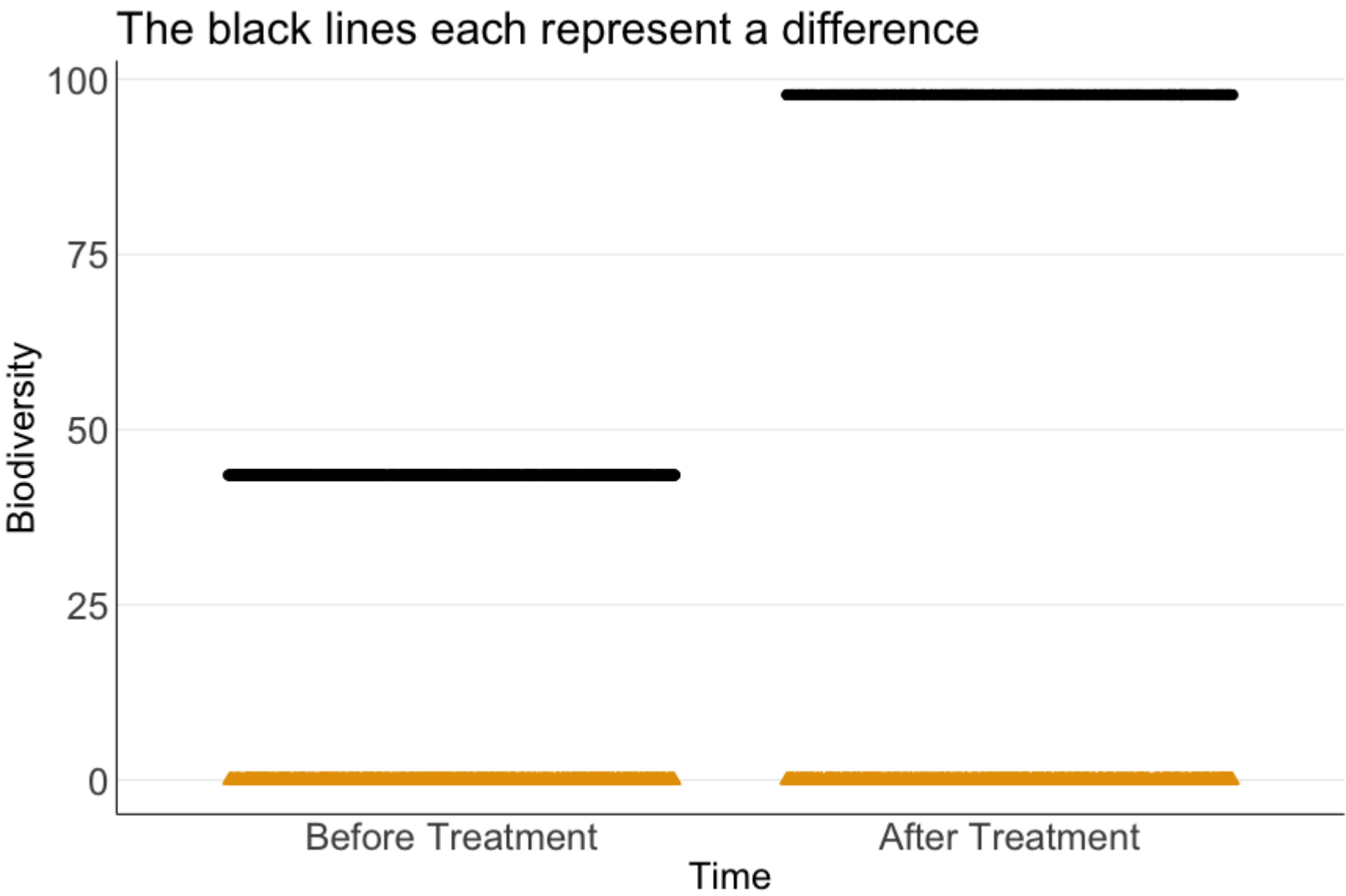
DD step 3



DD step 4

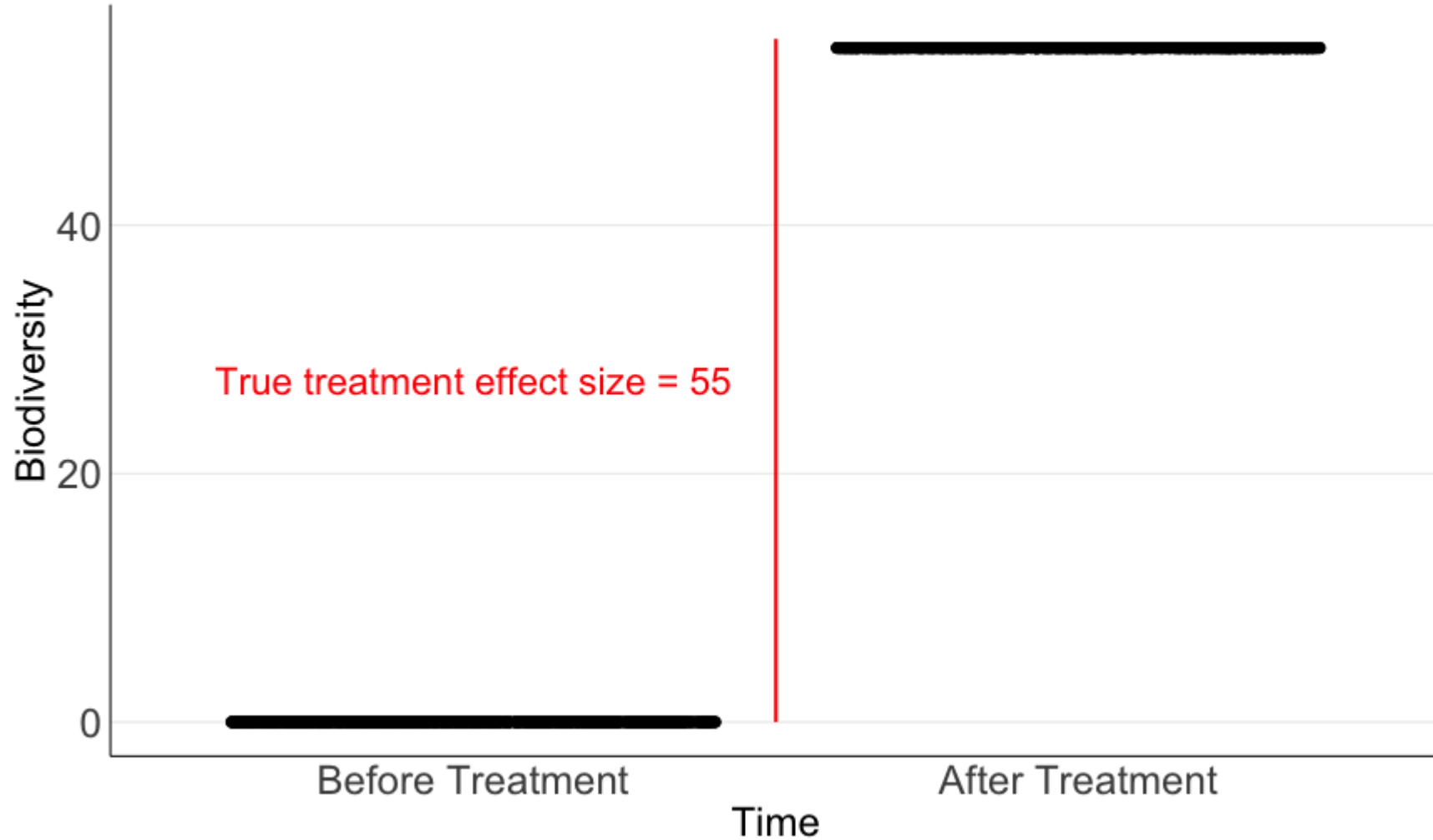


DD step 5



DD step 6

The remaining difference in the treatment group
is the difference-in-differences



The effect of leaded gasoline on elderly mortality: Evidence from regulatory exemptions

What is the paper about?

What is Hollingsworth and Rudik (2021) ([HR](#)) about?

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1. There is little causal evidence for any effects of lead

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Why is this important? We know lead is bad

1. There is little causal evidence for any effects of lead
2. Almost zero causal evidence for effects of lead on adults in any way
3. Having an accurate measure of effects/costs is vital for policymaking

Environmental research directly affects policy!

PUBLISHED DOCUMENT

AGENCY:

Environmental Protection Agency (EPA).

ACTION:

Notice; call for information.

SUMMARY:

The Environmental Protection Agency (EPA) is preparing an Integrated Science Assessment (ISA) as part of the review of the primary and secondary National Ambient Air Quality Standards (NAAQS) for Lead (Pb). The ISA will be completed by EPA's Office of Research and Development's Center for Public Health and Environmental Assessment (CPHEA). When final, the ISA is intended to update the previous Pb ISA (EPA/600/R-10/075F), published on June 26, 2013. Interested parties are invited to assist EPA in developing and refining the scientific information base for the review of the Pb NAAQS by submitting research studies and data that have been published, accepted for publication, or presented at a public scientific meeting since January 1, 2011.

DOCUMENT DETAILS

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[PDF](#)

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[Environmental Protection Agency](#)

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All communications and information should be received by EPA by September 8, 2020.

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Docket ID No. EPA-HQ-OAR-2020-0312
FRL-10011-92-ORD

Document Number:

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The quasi-experiment HR exploits is the sudden removal of lead from racing gasoline in 2007

Places that happened to have racetracks in 2007 had a significant decrease in lead emissions relative to places without racetracks

How does the paper do it?

Here's the 2x2 DD table

	Before	After
Treated	Areas near NASCAR racetracks before 2007	Areas near NASCAR racetracks after 2007
Control	Areas far from NASCAR racetracks before 2007	Areas far from NASCAR racetracks after 2007

We are comparing areas **close** vs far from racetracks, before vs after deleading in 2007

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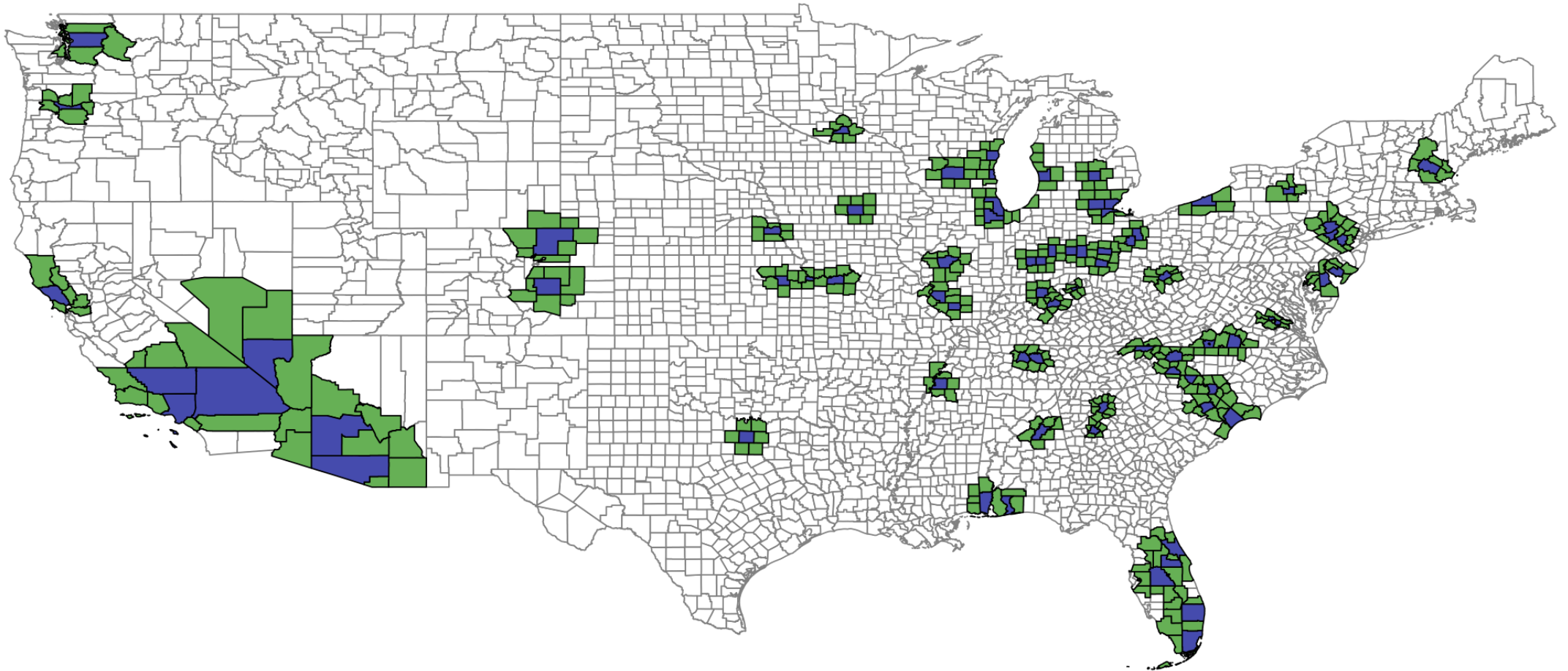
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How does the paper do it?

track/treated counties, border/weak treated counties, white control counties



Event studies

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1. We can look at dynamic effects
 2. It provides supporting evidence for the parallel trends assumption

Event studies: dynamic effects

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If we see estimates getting larger, the effect grows over time

If estimates get smaller, the effect shrinks

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We never observe what would have **actually** happened though, parallel pre-trends is just supporting evidence that the parallel trends assumption holds

HR (2021): to the data

Now lets use the actual HR (2021) data to get some practice: [notebook here](#)

HR (2021): takeaways

What can we take away from HR (2021)

1. Lead has a causal effect on elderly mortality
 - It appears to be through cardiovascular channels, perhaps *deaths of despair* as well (Case and Deaton, 2015)
2. The mortality costs are large
 - The external mortality costs imposed by NASCAR are larger than the value of all NASCAR teams combined
 - The social cost of lead is **at least \$1,000 per gram**
 - This is very, very, very big