EC 421, Set 10

Edward Rubin

# Prologue

## Schedule

### **Last Time**

Autocorrelation and nonstationarity

## Today

Causality

### Intro

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For the rest of the term, we will focus on **causally estimating**  $\beta_i$ .

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Many of these challenges relate to **exogeneity**, i.e.,  $E[u_i|X] = 0$ . Causality requires us to **hold all else constant** (ceterus paribus).

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- What causes some countries to grow and others to decline?
- What caused the capital riot?
- Did lax regulationcause Texas's recent energy problems?
- How does the number of police officers affect crime?
- What is the effect of better air quality on test scores?
- Do longer prison sentences decrease crime?
- How did cannabis legalization affect mental health/opioid addiction?

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#### **New saying:**

Correlation plus exogeneity is causation.

Let's work through a few examples.

## Example: The causal effect of fertilizer<sup>†</sup>

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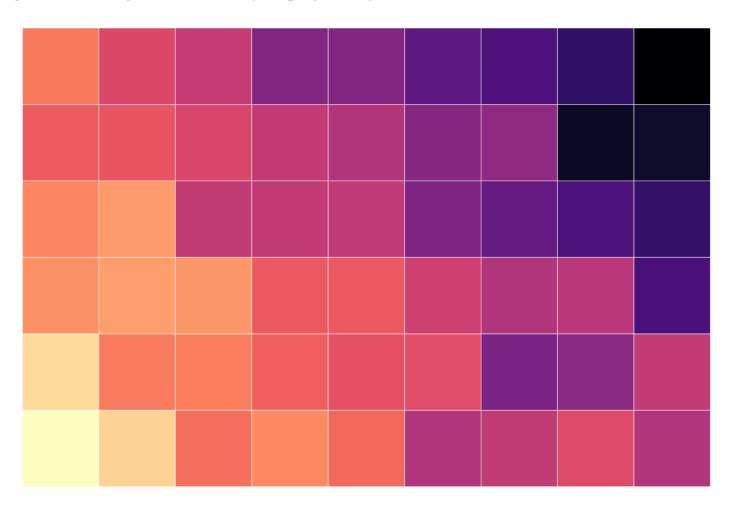
All else equal!

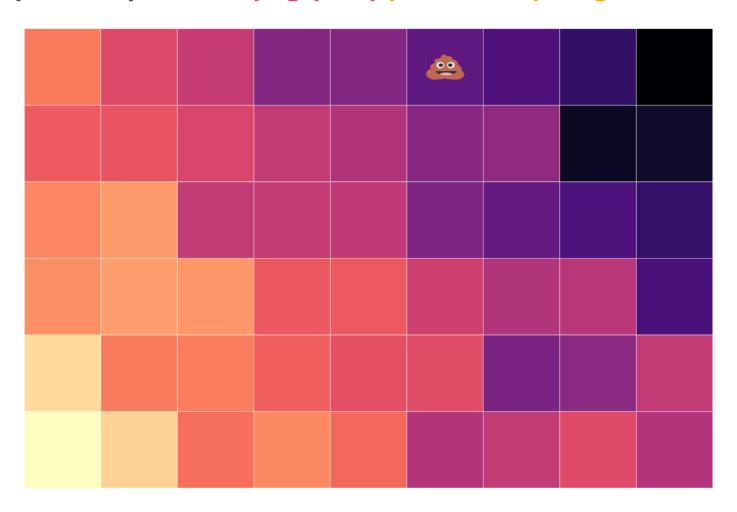
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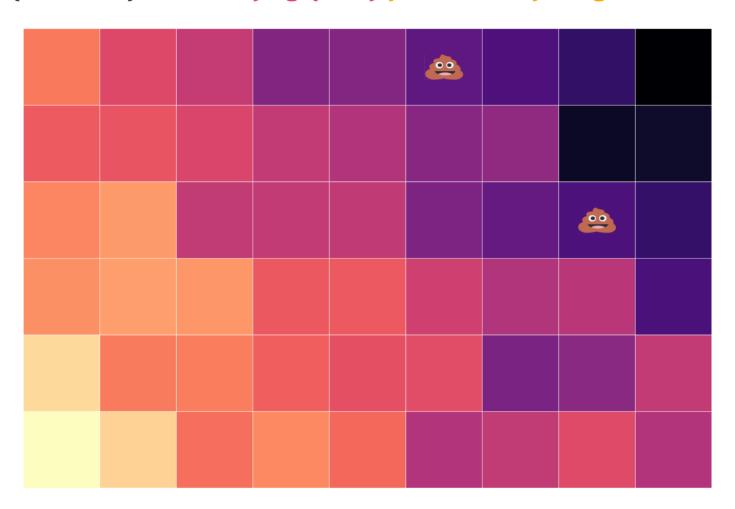
### 54 equal-sized plots

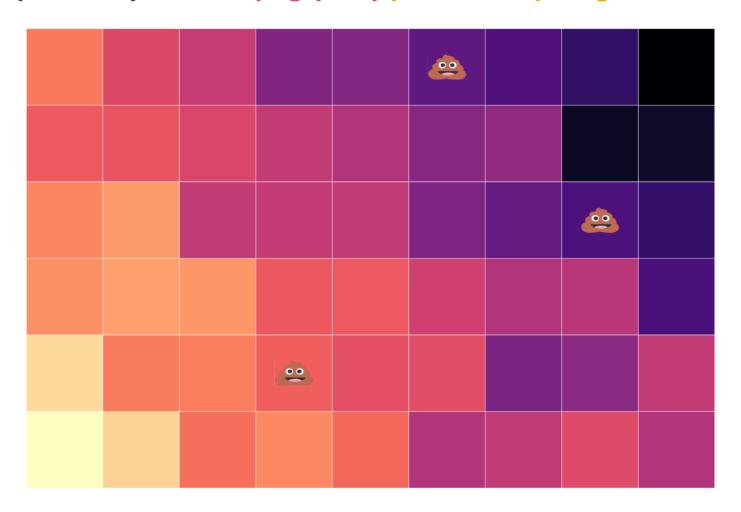
01	02	03	04	05	06	07	08	09
10	11	12	13	14	15	16	17	18
19	20	21	22	23	24	25	26	27
28	29	30	31	32	33	34	35	36
37	38	39	40	41	42	43	44	45
46	47	48	49	50	51	52	53	54

### 54 equal-sized plots of varying quality

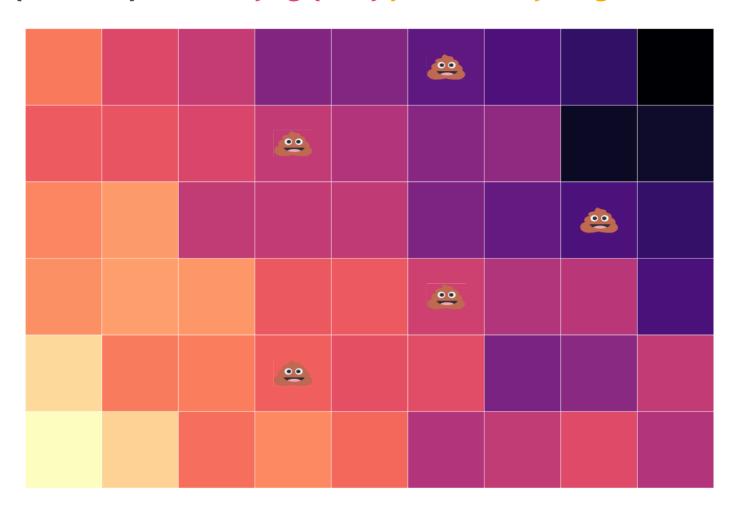


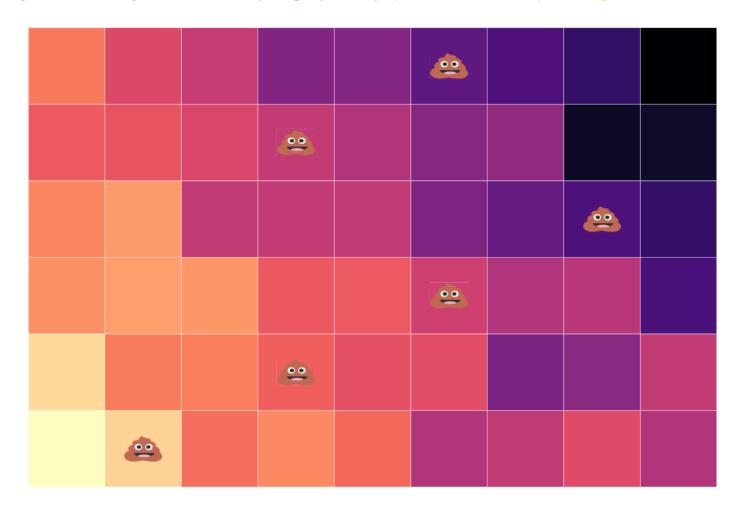


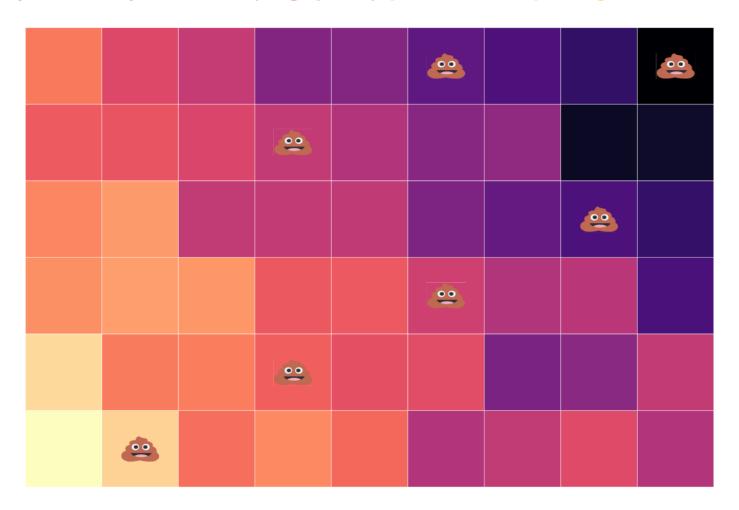


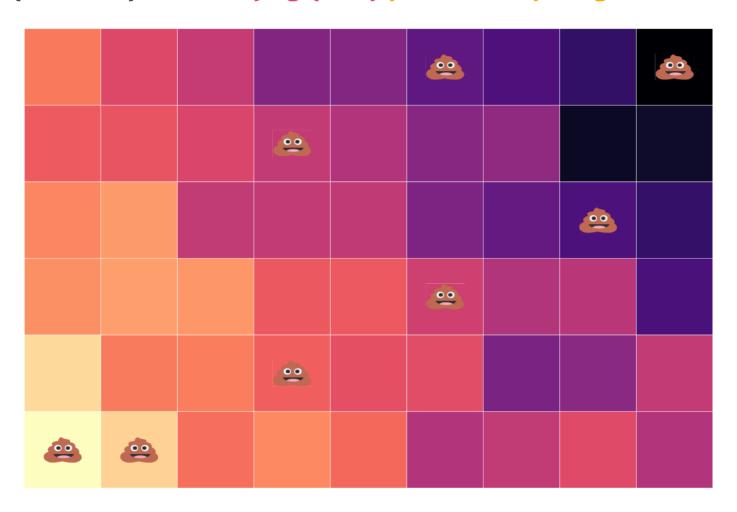


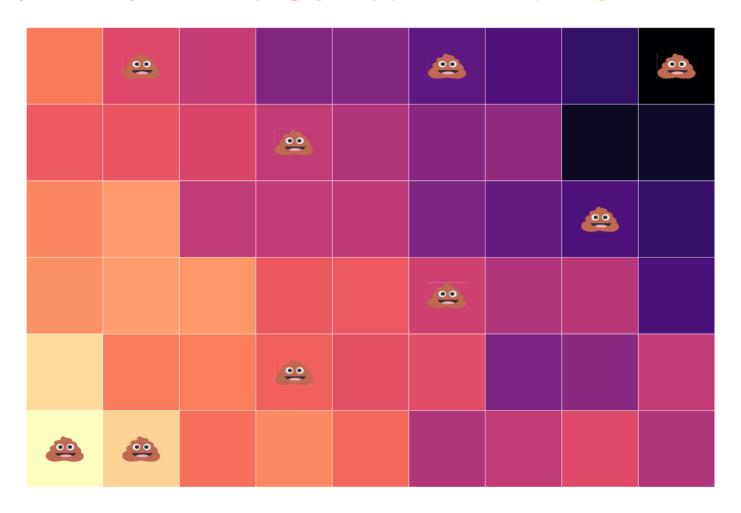


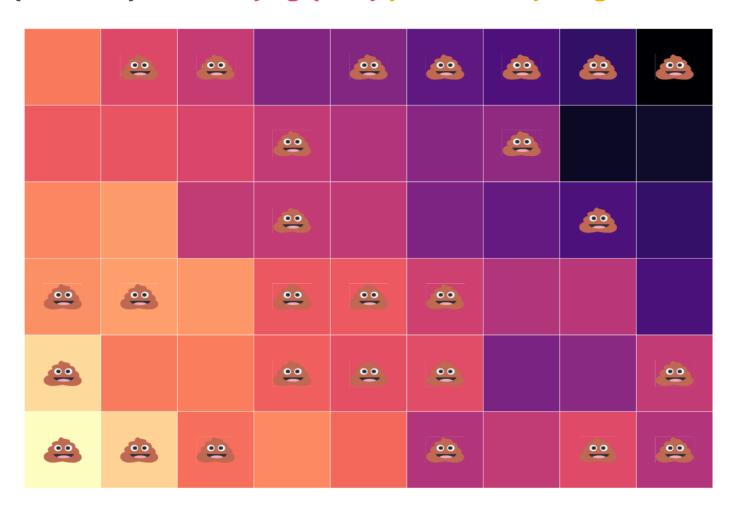


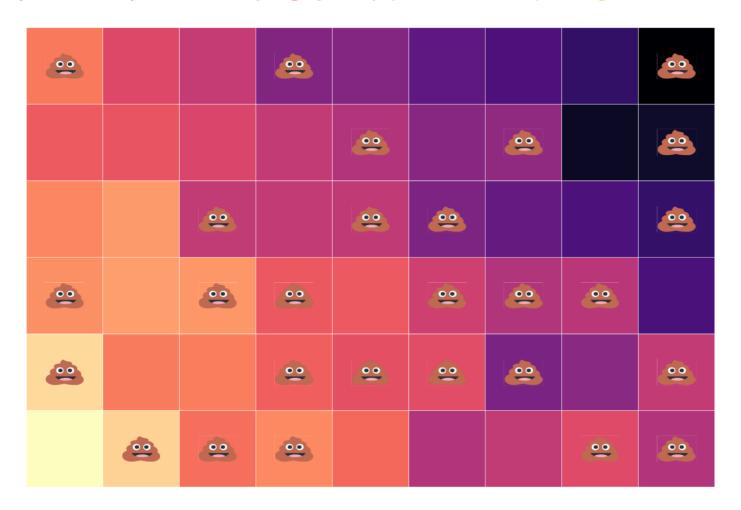


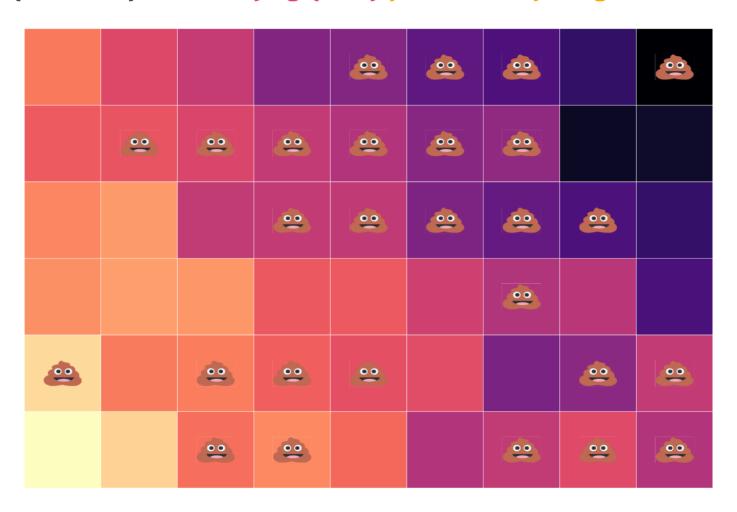












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**A:** On average, **randomly assigning treatment should balance** trt. and control across the other dimensions that affect yield (soil, slope, water).

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#### **Thought experiment:**

- Randomly select an individual.
- Give her an additional year of education.
- How much do her earnings increase?

This change in earnings gives the **causal effect** of education on earnings.

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The point (2) above also illustrates the difficulty in learning about educations while *holding all else constant*.

Many important variables have the same challenge—gender, race, income.

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- Admissions cutoffs
- Lottery enrollment and/or capacity constraints

### Real-world experiments

Both examples consider **real experiments** that isolate causal effects.

#### **Characteristics**

- Feasible—we can actually (potentially) run the experiment.
- Compare individuals randomized into treatment against individuals randomized into control.
- Require "good" randomization to get all else equal (exogeneity).

### Real-world experiments

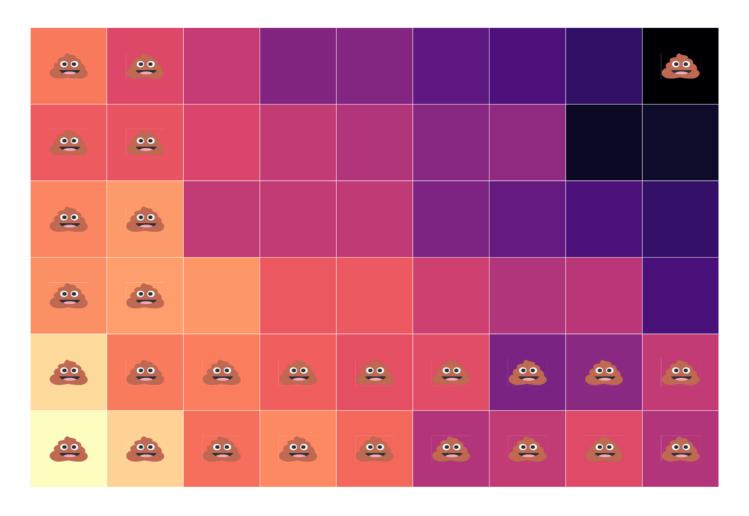
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- Compare individuals randomized into treatment against individuals randomized into control.
- Require "good" randomization to get all else equal (exogeneity).

Note: Your experiment's results are only as good as your randomization.

#### **Unfortunate randomization**



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This *ideal experiment* is clearly infeasible<sup>†</sup>, but it creates nice notation for causality (the Rubin causal model/Neyman potential outcomes framework).

† Without (1) God-like abilities and multiple universes or (2) a time machine.

### The ideal experiment

The ideal data for 10 people

```
i trt y1i y0i
#>
#> 1
          1 5.01 2.56
#> 2
      2 1 8.85 2.53
#> 3
      3 1 6.31 2.67
      4 1 5.97 2.79
#> 4
#> 5
      5 1 7.61 4.34
#> 6
      6 0 7.63 4.15
#> 7
         0 4.75 0.56
      8 0 5.77 3.52
#> 8
#> 9
         0 7.47 4.49
#> 10 10
         0 7.79 1.40
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Calculate the causal effect of trt.

$$\tau_i = y_{1,i} - y_{0,i}$$

for each individual i.

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      i trt y1i y0i effect i
#> 1
          1 5.01 2.56
                          2.45
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The mean of  $\tau_i$  is the average treatment effect (ATE).

Thus, 
$$\overline{ au}=3.82$$

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This model highlights the fundamental problem of causal inference.

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But, we do observe

- **y**<sub>1,i</sub> for *i* in 1, 2, 3, 4, 5
- $y_{0,j}$  for j in 6, 7, 8, 9, 10

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**Q:** How do we "fill in" the NA's and estimate  $\overline{\tau}$ ?

#### Causally estimating the treatment effect

**Notation:** Let  $D_i$  be a binary indicator variable such that

- $D_i = 1$  if individual i is treated.
- $D_i = 0$  if individual *i* is not treated (*control* group).

#### Causally estimating the treatment effect

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Then, rephrasing the previous slide,

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Note: We defined

$$au_i= au=y_{1,i}-y_{0,i}$$

which implies

$$y_{1,i} = y_{0,i} + \tau$$

$$= Avg(y_i \mid D_i = 1) - Avg(y_i \mid D_i = 0)$$

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Difference in groups' means

$$A = Avg(y_i \mid D_i = 1) - Avg(y_i \mid D_i = 0)$$

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So our proposed group-difference estimator give us the sum of

- 1.  $\tau$ , the causal, average treatment effect that we want
- 2. Selection bias: How much trt. and control groups differ (on average).

**Next time:** Solving selection bias.

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