

# EC 421

## Final

Spring 2019

**Full Name** ←

**UO ID** ← **KEY**

Total points:           /108

No phones, calculators, or outside materials.

## True/False

32.5 points

**Note:** You do not need to explain to your answers **in this section**.

01. [T/F] (2.5pts) In the presence of omitted-variable bias, ordinary least squares (OLS) is still consistent.

F

02. [T/F] (2.5pts) In the model  $\text{Births}_t = \beta_0 + \beta_1 \text{Income}_t + u_t$ , only the current period's income affects the current period's number of births.

T

03. [T/F] (2.5pts) In the model  $\text{Births}_t = \beta_0 + \beta_1 \text{Income}_t + \beta_2 \text{Income}_{t-1} + u_t$ , only the current period's income affects the current period's number of births.

F

04. [T/F] (2.5pts) In the model  $\text{Births}_t = \beta_0 + \beta_1 \text{Income}_t + \beta_2 \text{Births}_{t-1} + u_t$ , only the current period's income affects the current period's number of births.

F

05. [T/F] (2.5pts) If an estimator is biased, then it is not consistent.

F

06. [T/F] (2.5pts) As long as the mean of a variable does not change with time, the variable is stationary.

F

07. [T/F] (2.5pts) With a  $p$ -value of 0.049 and a significance level of 0.05, we reject the null hypothesis.

T

08. [T/F] (2.5pts) Random walk walks are stationary.

F

09. [T/F] (2.5pts) If the average *untreated* outcome ( ~~$E[Y_{0i}]$~~ ) in the treated group equals the average *untreated* outcome in the control group, then we do not need to worry about selection bias.

T

10. [T/F] (2.5pts) Exogeneity requires  $E[u_i^2] = \sigma^2$ .

F

11. [T/F] (2.5pts) Randomized experiments typically have issues with selection bias.

F

12. [T/F] (2.5pts) Causation has nothing to do with correlation.

F

13. [T/F] (2.5pts) Instrumental variables estimates can be consistent when OLS is inconsistent.

T

## Short definitions

33 points

14. (3pts) Define the "standard error of an estimator".

The standard error of an estimator gives the standard deviation of the estimator's distribution.

15. (3pts) Define "autocorrelation".

Autocorrelation means a variable is correlated with itself—e.g., an individual's previous outcomes/shocks correlate with current outcomes/shocks.

16. (3pts) Define "nonstationarity".

Nonstationarity means a random variable is "stable" (behaves well) throughout time.

Alternatively:

- Mean unaffected by time,  $E[X_t] = E[X_{t+k}] \forall k$
- Variance unaffected by time,  $\text{Var}(X_t) = \text{Var}(X_{t+k}) \forall k$
- Covariance unaffected by time,  $\text{Cov}(X_t, X_{t+k}) = \text{Cov}(X_s, X_{s+k}) \forall t, s, k$

17. (3pts) Define "p-value".

A p-value gives the probability of observing our outcome—or a more extreme outcome—under the null hypothesis.

18. (3pts) Define "causality".

Causality tells us the effect of an event by comparing the outcome of a universe w/ the event to the outcome in a universe w/out the event (the counterfactual).

19. (3pts) Define "selection bias".

Selection bias is a type of bias that occurs when our control group and treatment group are not comparable.

20. (3pts) Define "the fundamental problem of causal inference"

The fundamental problem of causal inference is that we cannot simultaneously observe  $Y_i$  (treated) and  $Y_i$  (control) for the same individual.

21. (3pts) What is a "random walk"?

A random walk is a time-series process such that

$$X_t = X_{t-1} + \varepsilon_t$$

(unnecessary: And  $\varepsilon_t$  is a stationary error term.)

22. (6pts) What are the two requirements for a *valid* instrument? Briefly define each requirement.

1. Exogenous: The instrument only affects  $Y_i$  (outcome) through  $X_i$  — not directly or through other variables.
2. Relevant: The instrument correlates w/ our variable of interest ( $X_i$ ).

23. (3pts) What is "heteroskedasticity"?

Heteroskedasticity occurs when the variance of our disturbance is not constant, i.e.,  $\text{Var}(\varepsilon_i) = \sigma_i^2$  and  $\sigma_i^2 \neq \sigma_j^2$  for some  $i, j$ .

Also will accept: when variance of the disturbance correlates w/ an explanatory variable.

May use  $u_i$ .

## Short answer

42.5 points

24. Suppose you want to estimate the causal effect of education on future earnings.

- a. (6pts) Explain why regressing earnings on education is not going to give you the answer you want (i.e., the causal effect of education on earnings).

Regressing earnings on education will likely suffer from omitted-variable bias (selection bias).

—

There are omitted variables that correlate w/ education AND affect earnings. This situation can lead to bias.

- b. (4pts) Now imagine you know there is a scholarship program that randomly gives out scholarships. Individuals who receive these scholarships. Explain how you could use instrumental variables to estimate the causal effect of education on earnings.

We could use 2SLS (or IV) where scholarship winning is our instrument for education.

✓ If they check this box, award 2 pts and move on to question 26.

Check this box if you want to skip all of question 25 and instead receive **2pts**.

**25.** Each part of this question refers to the following R output which results from estimating

```
lm(income ~ education + experience + female, data = wage_df)

#> # A tibble: 4 x 5
#>   term                estimate std.error statistic  p.value
#>   <chr>              <dbl>    <dbl>    <dbl>    <dbl>
#> 1 (Intercept)      3177.    2606.     1.22 2.26e- 1
#> 2 education         952.     109.     8.74 7.66e-14
#> 3 experience       2898.     89.0    32.6 1.10e-53
#> 4 female          -1761.    1570.    -1.12 2.65e- 1
```

**a. (2pts)** Write down the model that we've estimated (do not include the estimates, just the  $\beta$ s).

$$\text{income}_i = \beta_0 + \beta_1 \text{education}_i + \beta_2 \text{experience}_i + \beta_3 \text{female}_i + u_i$$

Note: must include disturbance for full credit.

**b. (3pts)** Carefully interpret the coefficient on education.

Holding all else constant, an additional year of education increases income by 952.

**c. (3pts)** Conduct a hypothesis test for the coefficient on education. Describe each step and the explain your conclusion.

Hypotheses -  $H_0: \beta_1 = 0$   $H_A: \beta_1 \neq 0$   
p-value -  $p\text{-value} = 7.66 \times 10^{-14} < 0.05 \therefore \text{Reject } H_0$   
Conclusion - There is statistically significant evidence at the 5% level that education affects income.

**d. (3pts)** Carefully interpret the coefficient on female (an indicator variable for female).

Holding all else equal, women make 1761 less than men.

**e. (2.5pts) True/False** Because the  $p$ -value on female is greater than 0.05, we can conclude there is no gender-based difference in income.

False.

f. (2pts) If we remove female from the regression, do you expect the  $R^2$  to increase or decrease? Explain your answer.

Decrease. Adding more variables increases  $R^2$  mechanically.

g. (3pts) What assumptions/conditions must be satisfied for us to be able to interpret the coefficient on education as causal?

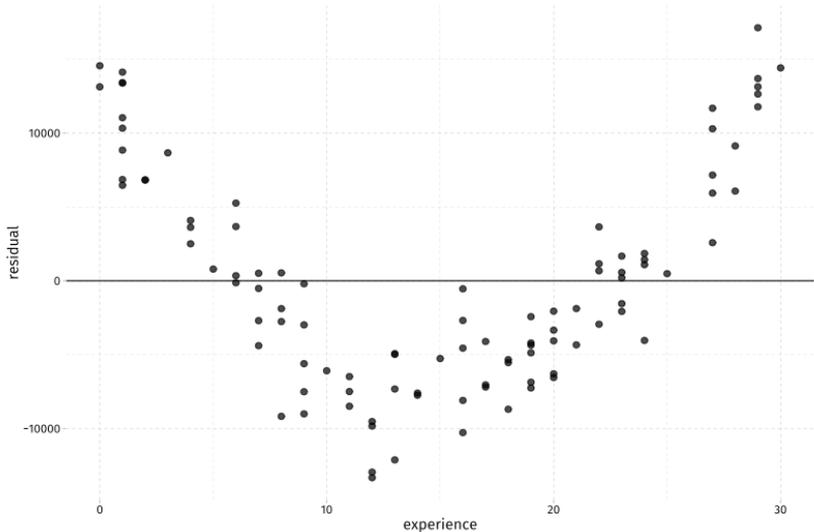
3 options:

Education must be exogenous

No selection bias

No omitted-variable bias

h. (2pts) Examine the following plot of the residuals from the previous regression (on the y axis) and experience (on the x axis). Describe any issues that suggests and how we might 'fix' them.



There is a trend in our residuals. This trend suggests misspecification.

Check this box if you want to skip all of question 26 and instead receive **2pts**.

**26.** Consider the following model for the number of alcoholic drinks an individual consumes in a day.

$$\text{Drinks}_t = \beta_0 + \beta_1 \text{Drinks}_{t-1} + \beta_2 \text{Income}_t + \beta_3 \text{Income}_{t-1} + u_t$$

**a. (2pts)** Carefully interpret the term  $\beta_1$ .

Holding all else constant, an additional drink yesterday increases the number of drinks today by  $\beta_1$ .

**b. (2pts)** Carefully interpret the term  $\beta_2$ .

Holding all else constant, an additional unit of income TODAY increases the number of drinks today by  $\beta_2$ .

**c. (2pts)** Carefully interpret the term  $\beta_3$ .

Holding all else constant, an additional unit of income YESTERDAY increases the number of drinks TODAY by  $\beta_3$ .

**d. (2pts)** What does  $\beta_2 + \beta_3$  tell us?

The total effect of income on # of drinks.

**e. (2pts)** What does this model assume about the effect of income throughout time?

Income has no effect on drinking after  $t-1$  (two days).

**f. (2pts)** What happens to our OLS-based estimate of  $\beta_1$  if  $u_t$  is autocorrelated?

Biased and inconsistent